

CS769 Advanced NLP

# Deep Learning Basic

Junjie Hu



Slides adapted from Graham  
<https://junjiehu.github.io/cs769-spring22/>

# Logistics

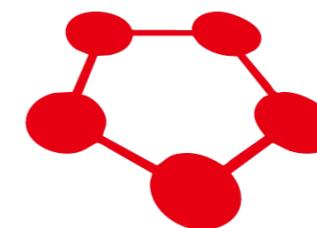
- HW1 is released.
- Office hour is updated to Friday 2:30-3:30 PM (Prof. Junjie Hu)
- Bonus point on Piazza
- Quiz will be submitted to Canvas.

# Neural Network Frameworks

theano

ay/net

Caffe



Chainer

mxnet

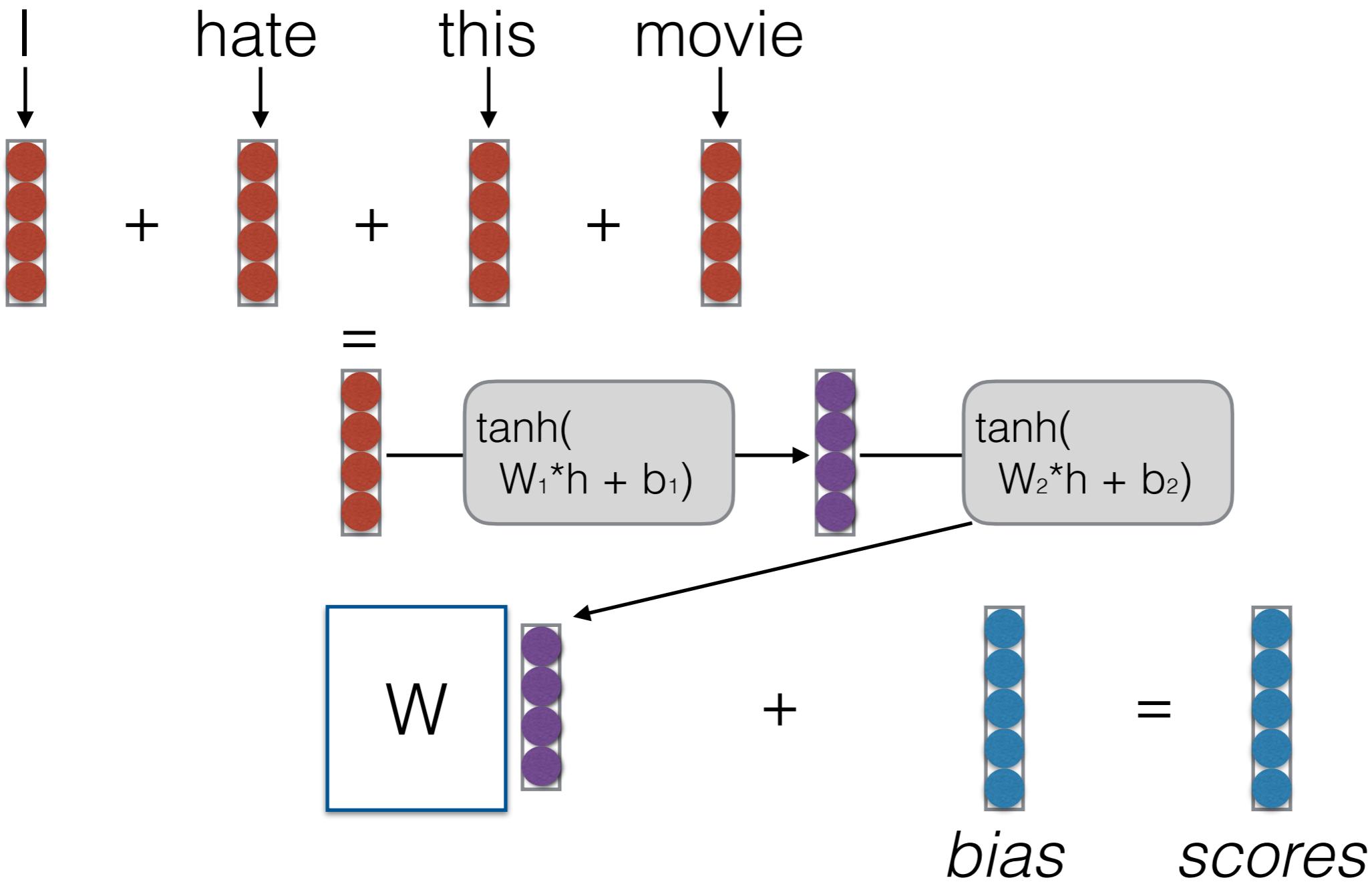
PYTORCH



TensorFlow



# Example App: Deep CBOW Model



# Algorithm Sketch for NN App Code

- Create a model
- For each example
  - **create a graph** that represents the computation you want
  - **calculate the result** of that computation
  - if training
    - perform **back propagation**
    - **update** parameters

# Tensors and Numerical Computation

# Numerical Computation Backend

- Most neural network libraries use a backend for numerical computation
- **PyTorch/Tensorflow:** MKL, CUDNN, CUDA, OpenMP, custom-written kernels
- Support many numerical functions on **tensors**

```
import torch
import torch.nn as nn
print(*torch.__config__.show().split("\n"), sep="\n")
```

PyTorch built with:

- GCC 7.3
- C++ Version: 201402
- Intel(R) Math Kernel Library Version 2020.0.0 Prod
- Intel(R) MKL-DNN v2.2.3 (Git Hash 7336ca9f055cf1b)
- OpenMP 201511 (a.k.a. OpenMP 4.5)
- LAPACK is enabled (usually provided by MKL)
- NNPACK is enabled
- CPU capability usage: AVX2
- CUDA Runtime 11.1
- NVCC architecture flags: -gencode;arch=compute\_37
- CuDNN 8.0.5
- Magma 2.5.2
- Build settings: BLAS\_INFO=mkl, BUILD\_TYPE=Release

# Tensors

- An n-dimensional array

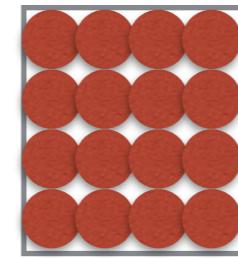
**Scalar**



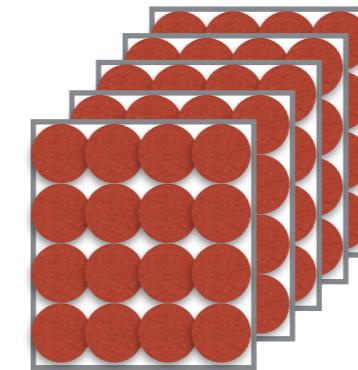
**Vector**



**Matrix**



**3-dim Tensor**



...

$$x \in \mathbb{R}$$

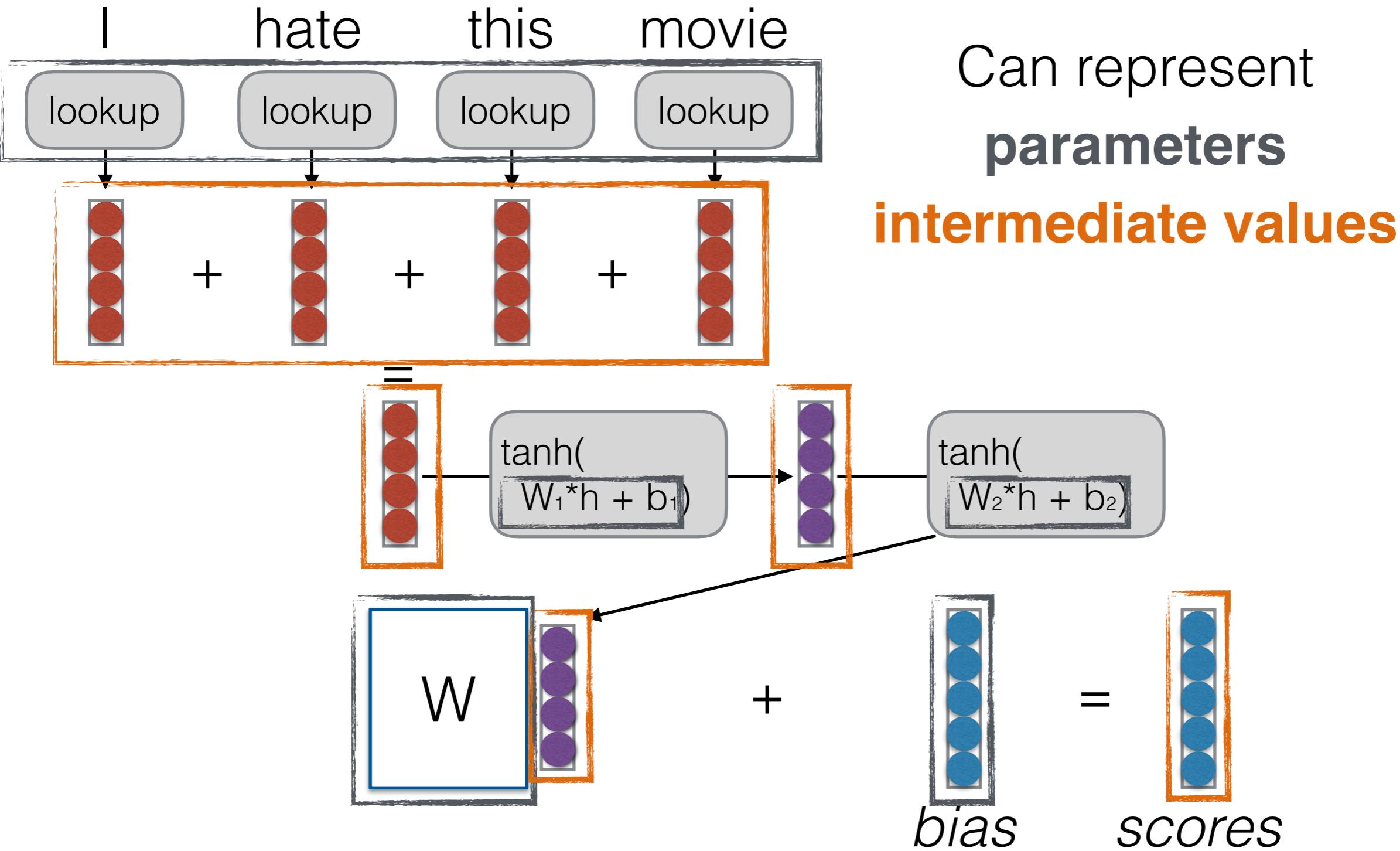
$$\mathbf{x} \in \mathbb{R}^4$$

$$\mathbf{X} \in \mathbb{R}^{4 \times 4}$$

$$\mathbf{X} \in \mathbb{R}^{4 \times 4 \times 5}$$

- Widely used in neural networks
- Parameters in NNs consist of different shape of tensors, which store both their **values** and **gradients**

# Tensors in Neural Networks



Can represent  
parameters

intermediate values

# Tensor Operations

- **PyTorch/Tensorflow:** Support many different matrix operations: matrix-multiply

```
import numpy as np
x = torch.Tensor([[2, 3], [1, 2]])
x = torch.Tensor(np.array([[-1, 1], [2, 4]]))
x = torch.zeros([2, 3], dtype=torch.int32)
```

create tensors from list, numpy.array

```
▶ import torch
    import torch.nn as nn

    x = torch.randn(4, 2)
    w = torch.randn(3, 4)
    print(x)
    print(w)

    tensor([[-1.5372,  0.0845],
           [ 0.5752,  0.7634],
           [ 0.4265, -0.1287],
           [-1.8629, -0.8520]])
    tensor([[-1.1272, -1.1810,  0.0867,  0.0676],
           [-0.1070,  3.2586,  0.7446, -1.2094],
           [-1.7670,  0.2900, -1.0881, -1.5555]])

[10] torch.matmul(w, x)  # results in a [3,2] matrix

    tensor([[ 0.9646, -1.0656],
           [ 4.6092,  3.4132],
           [ 5.3167,  1.5373]])
```

matrix multiply

```
▶ x = torch.randn(4,2)
    z = torch.randn(4,2)
    print(x)
    print(z)

    tensor([[ 0.0762,  1.5145],
           [-0.4747, -0.9141],
           [ 0.7106,  0.4888],
           [ 0.6959, -0.5305]])
    tensor([[ -0.1766,  0.6187],
           [ 0.9254, -0.5931],
           [ -0.9162,  0.3209],
           [ 0.0216, -0.7116]])
```

```
[13] x * z  # results in a [4,2] matrix
```

```
tensor([[ -0.0135,  0.9371],
           [ -0.4392,  0.5421],
           [ -0.6510,  0.1569],
           [  0.0151,  0.3775]])
```

Element-wise matrix multiply

# Model and Parameter Definition

# Algorithm Sketch

- Create a model
- For each example
  - **create a graph** that represents the computation you want
  - **calculate the result** of that computation
  - if training
    - perform **back propagation**
    - **update** parameters

# Example Model Creation

- Define model's parameters:
  - Weight matrix  $W_0$  for the input embedding layer
  - Weight matrix  $W_1, W_2$  and  $B_1, B_2$  for feedforward layers
  - Any other layers ...

```
class DanModel(BaseModel):  
    def __init__(self, args, vocab, tag_size):  
        super(DanModel, self).__init__(args, vocab, tag_size)  
        self.define_model_parameters()  
        self.init_model_parameters()  
  
        # Use pre-trained word embeddings if emb_file exists  
        if args.emb_file is not None:  
            self.copy_embedding_from_numpy()  
  
    def define_model_parameters():  
        """  
        Define the model's parameters, e.g., embedding layer,  
        """  
        raise NotImplementedError()
```

# Parameter Initialization

- Neural nets must have weights that are not identical to learn non-identical features
- **Uniform Initialization:** Initialize weights in some range, such as  $[-\nu, \nu]$ ,  $\nu = 0.01$  for example
  - *Problem!* Depending on the size of the net, inputs to downstream nodes may be very large
- **Glorot (Xavier) Initialization, He Initialization:** Initialize based on the size of the matrix

Glorot Init:  $\nu = \sqrt{\frac{6}{d_{\text{in}} + d_{\text{out}}}}$

# Example Model Initialization

- Initialize model's parameters using **Glorot** or others:
  - Create initial random values within  $[-v, v]$  for tensors such as  $W_0, W_1, W_2, B_1, B_2$  , and any others before training.

```
def init_model_parameters(self):  
    """  
        Initialize the model's parameters by uniform sampling from a range [-v, v]  
    """  
    raise NotImplementedError()
```

# Computation Definition

# NN App Algorithm Sketch

- Create a model
- For each example
  - **create a graph** that represents the computation you want
  - **calculate the result** of that computation
- if training
  - perform **back propagation**
  - **update** parameters

expression:

**x**

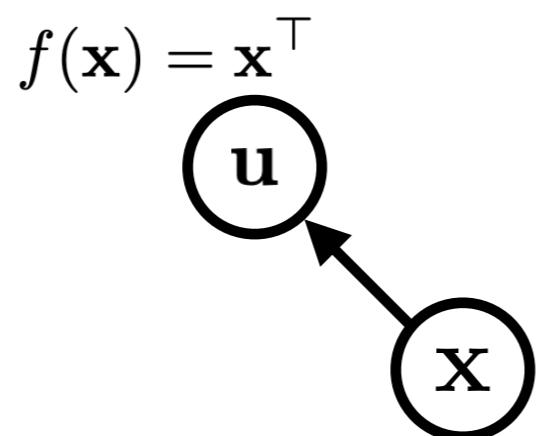
graph:



expression:

$$\mathbf{x}^\top$$

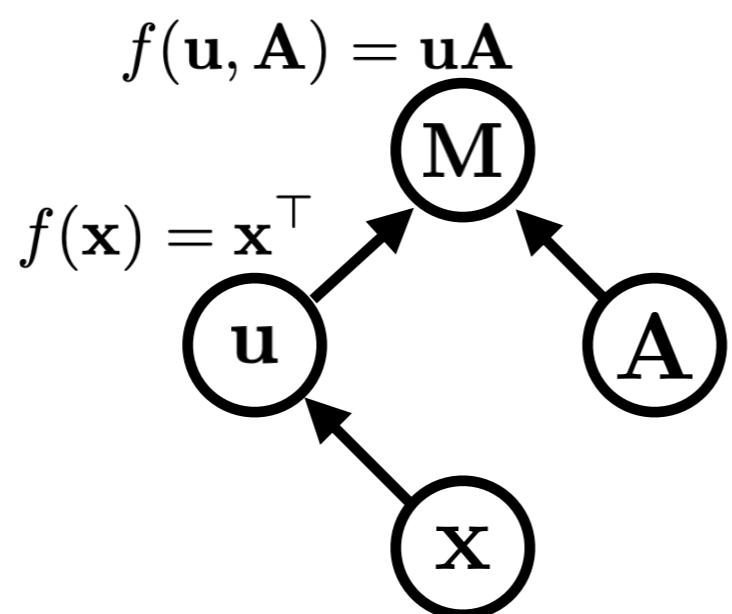
graph:



expression:

$$\mathbf{x}^\top \mathbf{A}$$

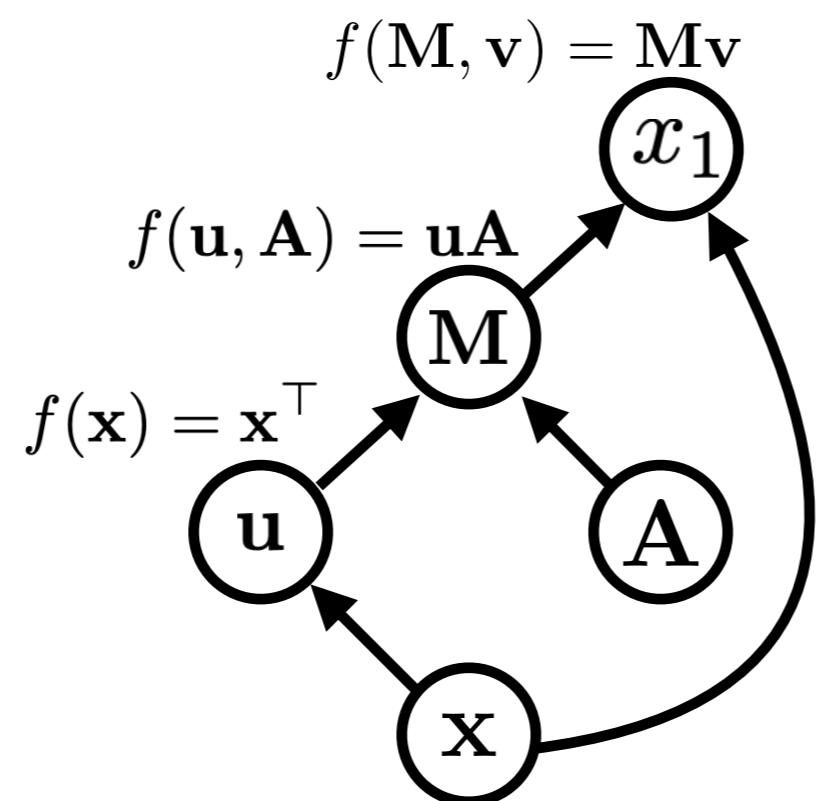
graph:



expression:

$$\mathbf{x}^\top \mathbf{A} \mathbf{x}$$

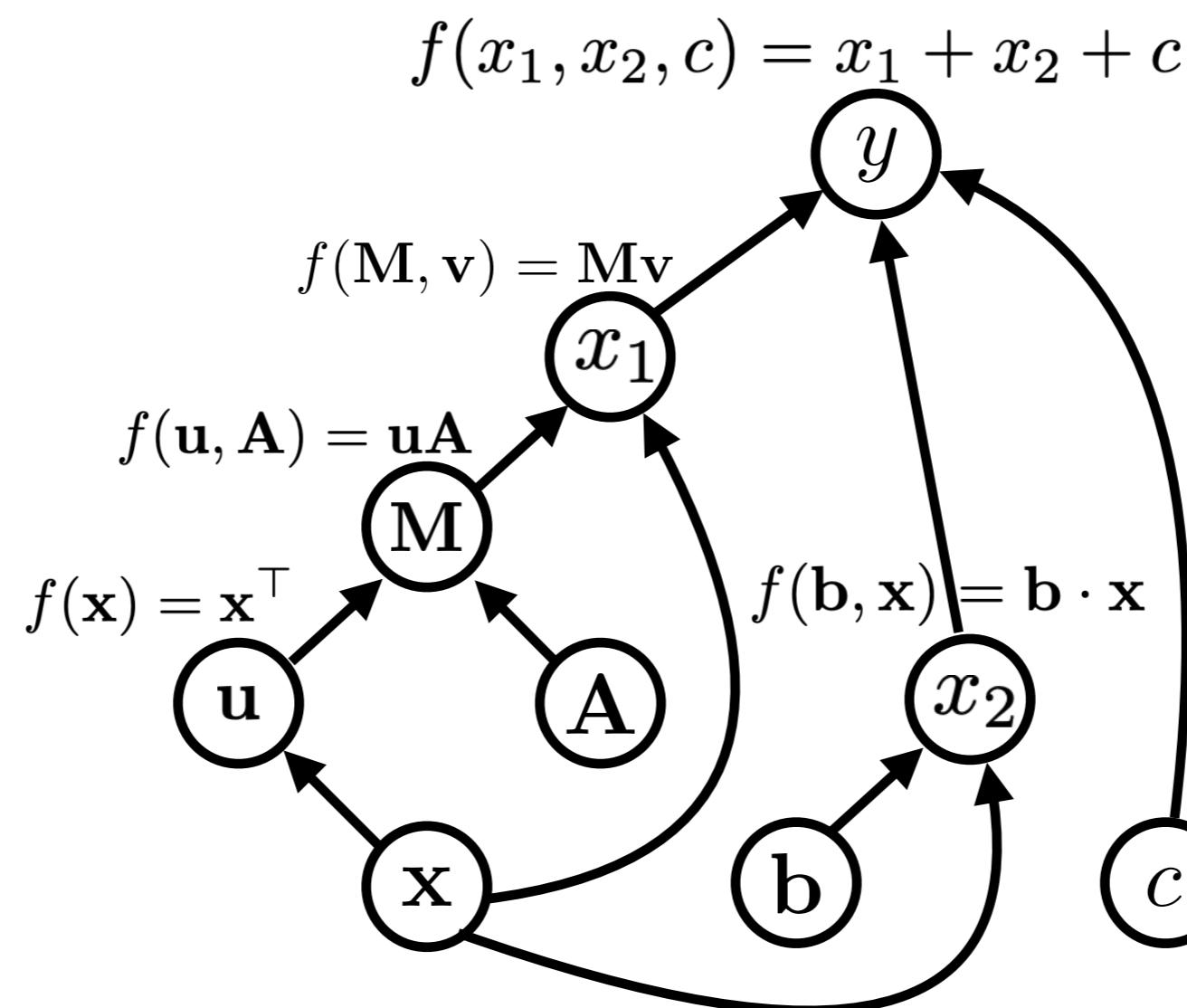
graph:



expression:

$$\mathbf{x}^\top \mathbf{A} \mathbf{x} + \mathbf{b} \cdot \mathbf{x} + c$$

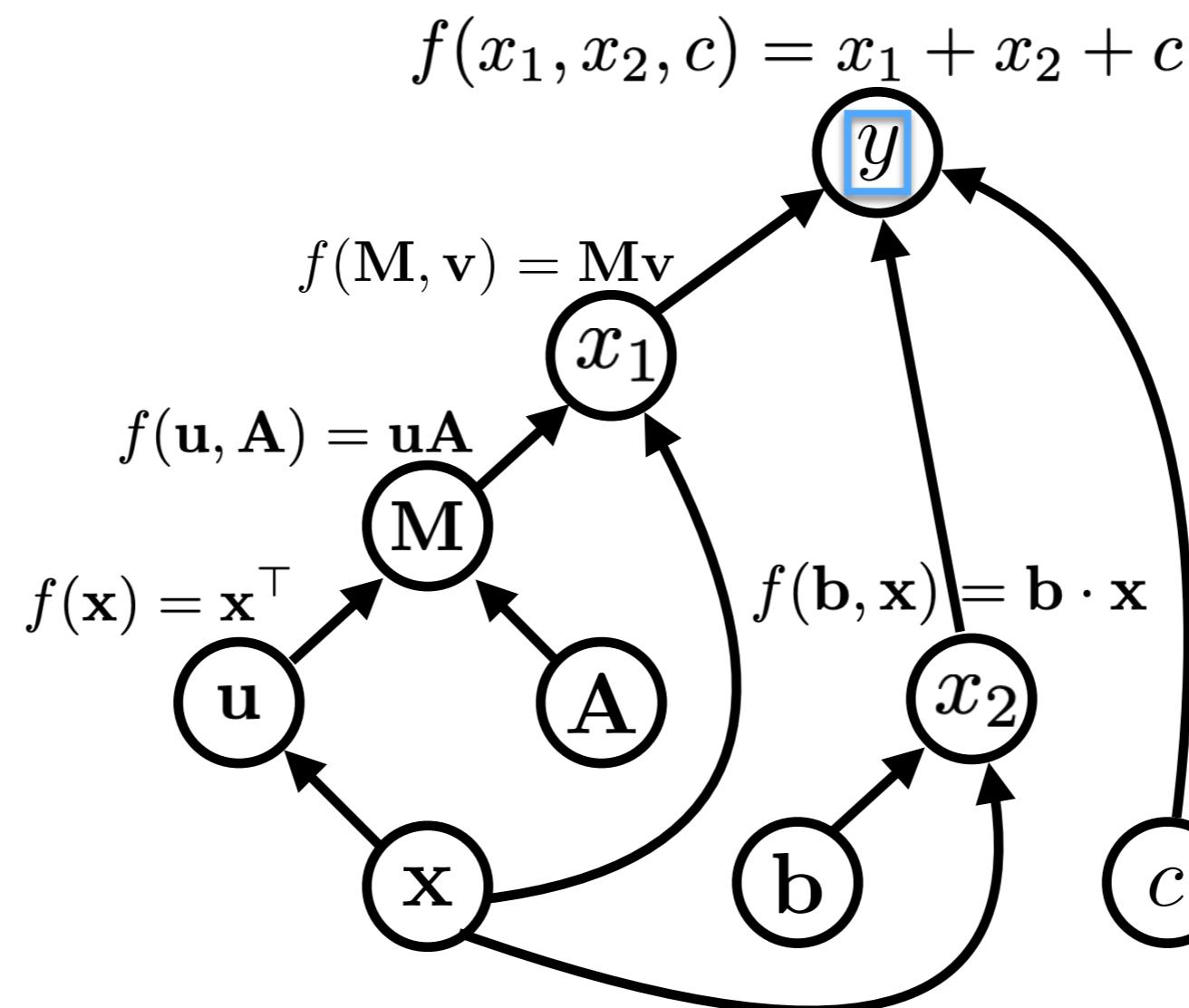
graph:



expression:

$$y = \mathbf{x}^\top \mathbf{A}\mathbf{x} + \mathbf{b} \cdot \mathbf{x} + c$$

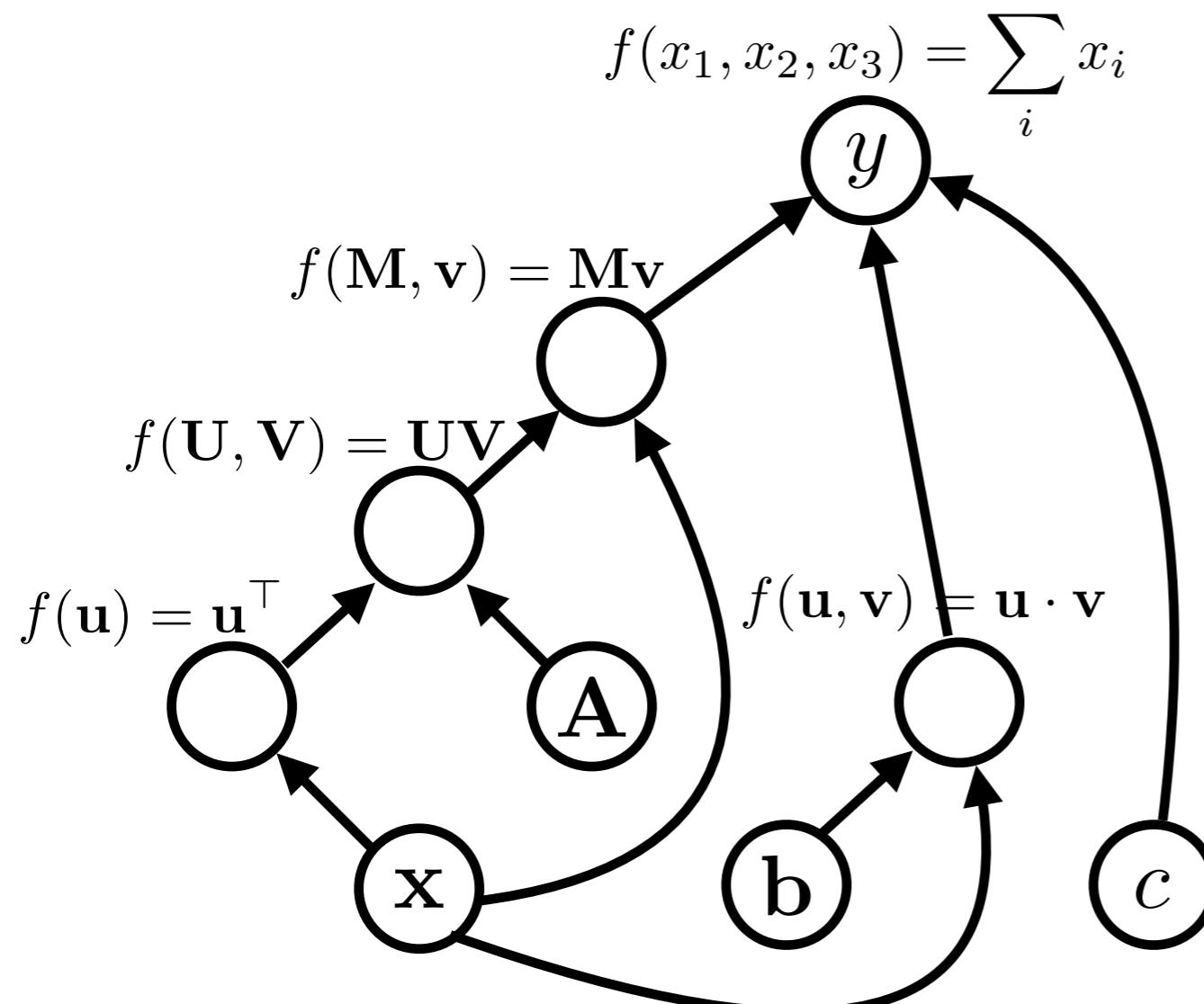
graph:



expression:

$$y = \mathbf{x}^\top \boxed{\mathbf{A}\mathbf{x}} + \boxed{\mathbf{b} \cdot \mathbf{x}} + \boxed{c}$$

graph:



```
# x: 5-dimensional vector
# Model's parameters contain:
#   A: 5x5 matrix
#   b: 5-dimensional vector
#   c: scalar

class SimpleModel(nn.Module):
    def __init__(self):
        super(SimpleModel, self).__init__()
        self.define_model_parameters()

    def define_model_parameters(self):
        self.A = nn.Parameter(torch.randn((5,5)))
        self.b = nn.Parameter(torch.randn((5)))
        self.c = nn.Parameter(torch.randn((1)))

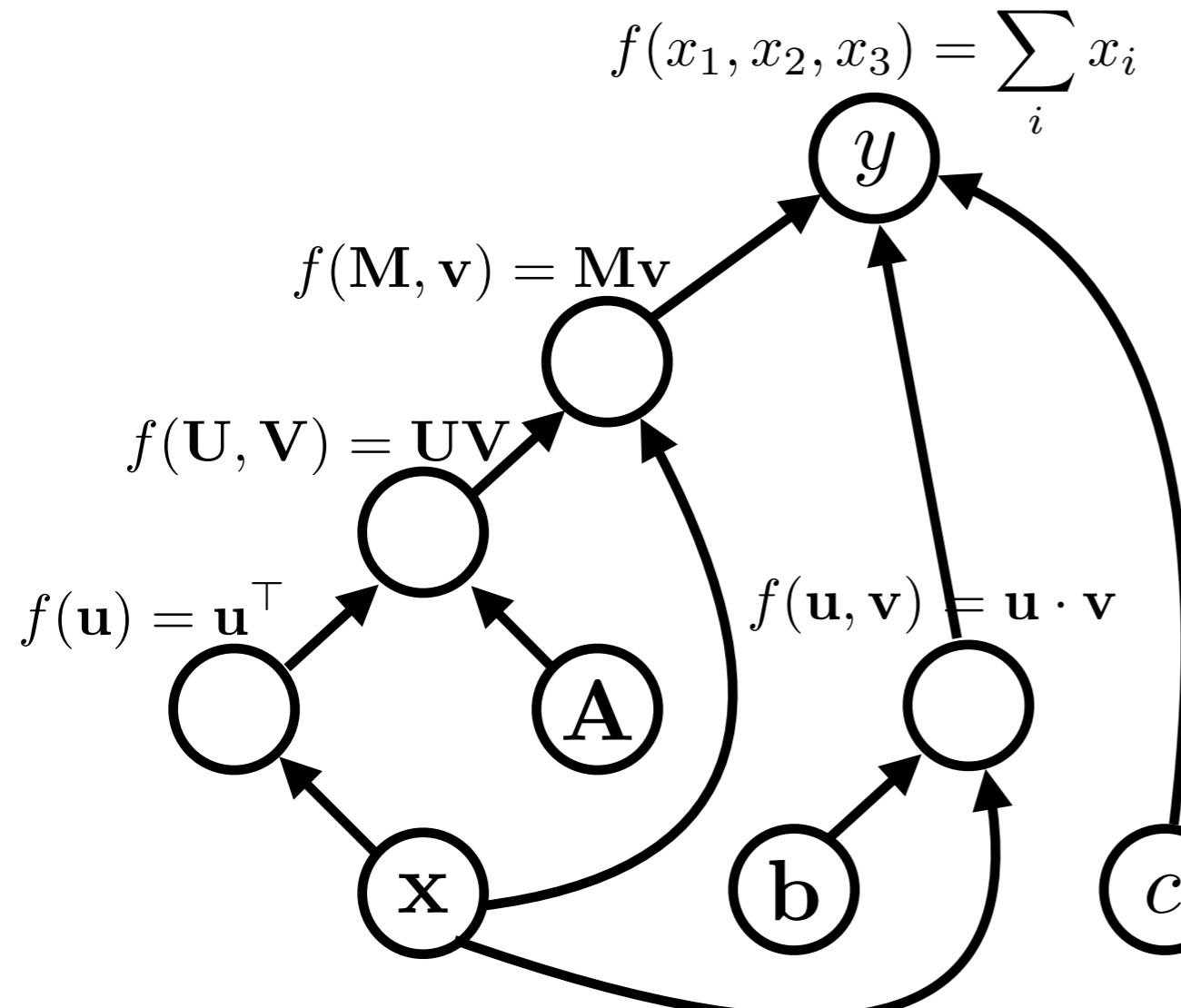
    def forward(self, x):
        U = x.T
        print('U', U)
        M = torch.matmul(U, self.A)
        print('M', M)
        Mv = torch.matmul(M, x)
        print('Mv', Mv)
        bx = torch.dot(self.b, x)
        print('bx', bx)
        y = Mv + bx + self.c
        return y

x = torch.randn(5)
model = SimpleModel()
y = model(x)
print(y)
```

expression:

$$y = \mathbf{x}^\top \mathbf{A} \mathbf{x} + \mathbf{b} \cdot \mathbf{x} + c$$

graph:



```
# x: 5-dimensional vector
# Model's parameters contain:
#   A: 5x5 matrix
#   b: 5-dimensional vector
#   c: scalar

class SimpleModel(nn.Module):
    def __init__(self):
        super(SimpleModel, self).__init__()
        self.define_model_parameters()

    def define_model_parameters(self):
        self.A = nn.Parameter(torch.randn((5,5)))
        self.b = nn.Parameter(torch.randn((5)))
        self.c = nn.Parameter(torch.randn((1)))

    def forward(self, x):
        U = x.T
        print('U', U)
        M = torch.matmul(U, self.A)
        print('M', M)
        Mv = torch.matmul(M, x)
        print('Mv', Mv)
        bx = torch.dot(self.b, x)
        print('bx', bx)
        y = Mv + bx + self.c
        return y

x = torch.randn(5)
model = SimpleModel()
y = model(x)
print(y)
```

# Operations

- Operations must know:
- **Forward:** how to calculate their value given input

$$f(\mathbf{u})$$

- **Backward:** how to calculate their derivative given following derivative

$$\frac{\partial f(\mathbf{u})}{\partial \mathbf{u}} \frac{\partial \mathcal{F}}{\partial f(\mathbf{u})}$$

# Back Propagation

# NN App Algorithm Sketch

- Create a model
- For each example
  - **create a graph** that represents the computation you want
  - **calculate the result** of that computation
  - if training
    - perform **back propagation**
    - **update** parameters

# Back Propagation

graph:

- Mean-square error:  $\mathcal{L} = (y - y^*)^2$

$$f(x_1, x_2, c) = x_1 + x_2 + c$$

$$\frac{\partial \mathcal{L}}{\partial y} = 2(y - y^*)$$

$$\frac{\partial \mathcal{L}}{\partial x_1} = \frac{\partial \mathcal{L}}{\partial y} \cdot \frac{\partial y}{\partial x_1} = 2(y - y^*)$$

$$\frac{\partial \mathcal{L}}{\partial \mathbf{M}} = \frac{\partial \mathcal{L}}{\partial x_1} \cdot \frac{\partial x_1}{\partial \mathbf{M}} = 2(y - y^*)\mathbf{x}$$

$$\boxed{\frac{\partial \mathcal{L}}{\partial \mathbf{A}} = \frac{\partial \mathcal{L}}{\partial \mathbf{M}} \cdot \frac{\partial \mathbf{M}}{\partial \mathbf{A}} = 2(y - y^*)\mathbf{x}\mathbf{x}^\top}$$

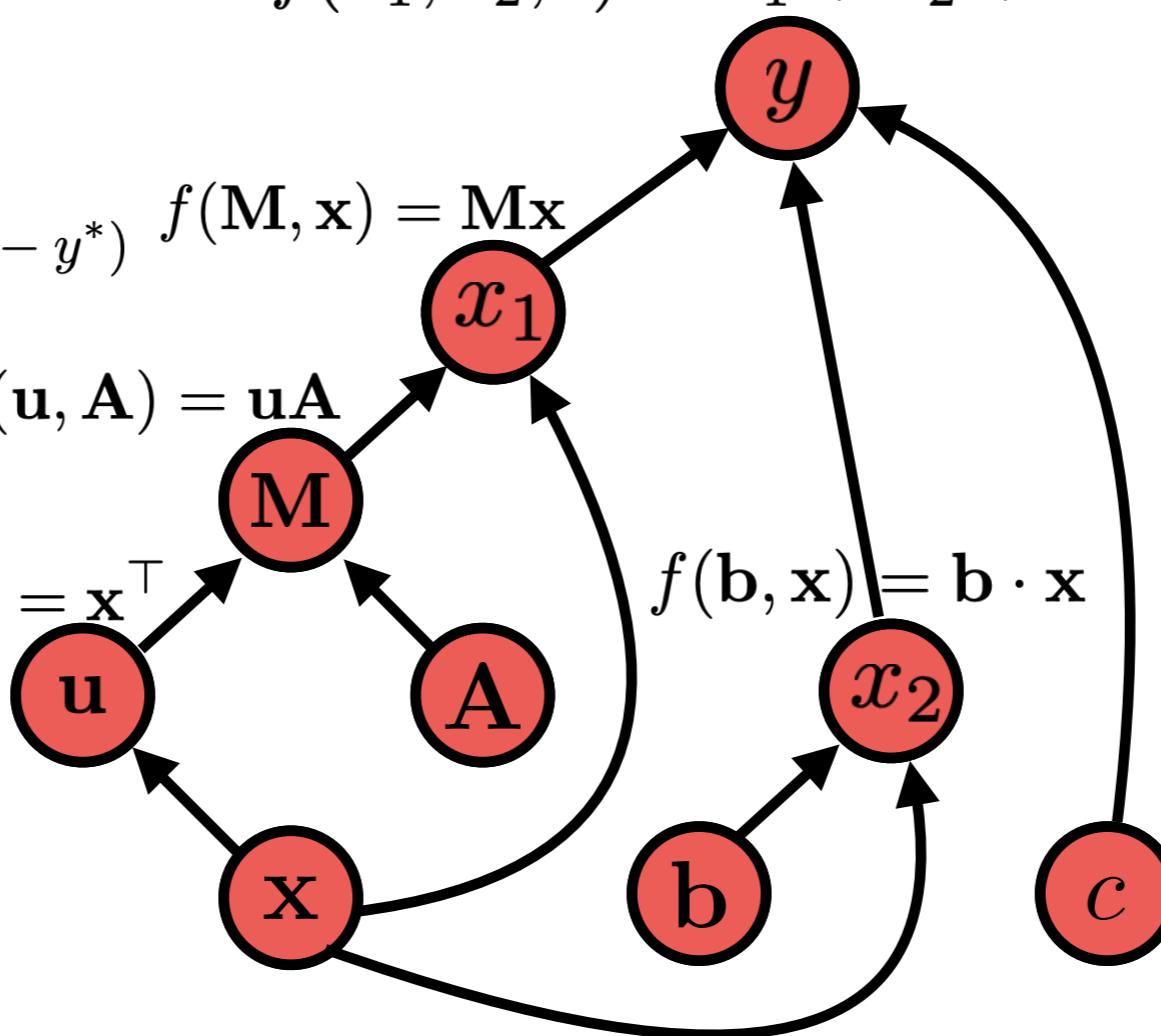
$$f(\mathbf{u}, \mathbf{A}) = \mathbf{u}\mathbf{A}$$

$$f(\mathbf{x}) = \mathbf{x}^\top$$

$$f(\mathbf{b}, \mathbf{x}) = \mathbf{b} \cdot \mathbf{x}$$

$$\frac{\partial \mathcal{L}}{\partial x_2} = \frac{\partial \mathcal{L}}{\partial y} \cdot \frac{\partial y}{\partial x_2} = 2(y - y^*)$$

$$\boxed{\frac{\partial \mathcal{L}}{\partial c} = \frac{\partial \mathcal{L}}{\partial y} \cdot \frac{\partial y}{\partial c} = 2(y - y^*)}$$



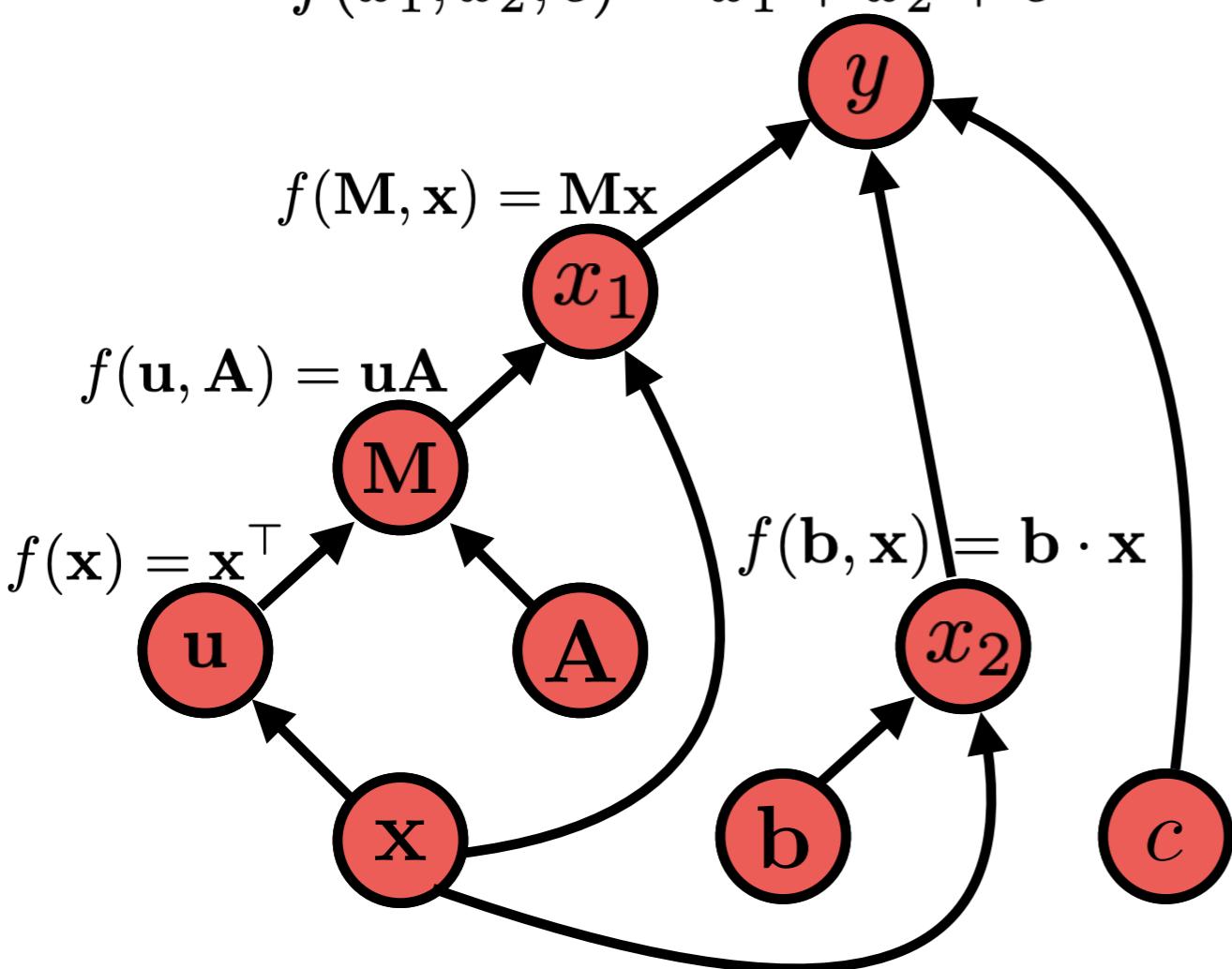
Model parameters:  $\mathbf{A}, \mathbf{b}, c$

$$\boxed{\frac{\partial \mathcal{L}}{\partial \mathbf{b}} = \frac{\partial \mathcal{L}}{\partial x_2} \cdot \frac{\partial x_2}{\partial \mathbf{b}} = 2(y - y^*)\mathbf{x}}$$

# Back Propagation

graph:

$$f(x_1, x_2, c) = x_1 + x_2 + c$$



- Mean-square error:  $\mathcal{L} = (y - y^*)^2$

```

▶ optimizer = torch.optim.Adagrad(model.parameters(), lr=0.01)
▶ loss_func = nn.MSELoss()

y_true = torch.FloatTensor([1.0]) # ground true
loss = loss_func(y, y_true)
print(loss)

⇒ tensor(34.0528, grad_fn=<MseLossBackward0>)
  
```

- Compute gradients automatically by most tools:  $\frac{\partial \mathcal{L}}{\partial A}, \frac{\partial \mathcal{L}}{\partial b}, \frac{\partial \mathcal{L}}{\partial c}$

```

▶ optimizer.zero_grad()
▶ loss.backward(retain_graph=True)
for name, param in model.named_parameters():
    print(name, param.grad)

⇒ A tensor([[ -0.0313,  -0.0386,  -0.8571,   0.7265,   0.9405],
           [ -0.0386,  -0.0476,  -1.0572,   0.8961,   1.1601],
           [ -0.8571,  -1.0572, -23.4711,  19.8953,  25.7557],
           [  0.7265,   0.8961,  19.8953, -16.8643, -21.8319],
           [  0.9405,   1.1601,  25.7557, -21.8319, -28.2627]])
b tensor([  0.6044,   0.7455,  16.5508, -14.0294, -18.1619])
c tensor([-11.6710])
  
```

# Parameter Update

# NN App Algorithm Sketch

- Create a model
- For each example
  - **create a graph** that represents the computation you want
  - **calculate the result** of that computation
  - if training
    - perform **back propagation**
    - **update** parameters

# Optimizer Update

- Most deep learning toolkits implement the parameter updates by calling **optimizer.step()** function

```
[59] # Before gradient update
    for name, param in model.named_parameters():
        print(name, param)

A Parameter containing:
tensor([[-0.2267,  0.6521, -0.8193,  0.7723, -0.6456],
       [ 1.2410, -2.4380, -0.5612, -0.1144, -0.2687],
       [ 0.4792,  0.4543, -1.3530,  1.2934, -0.9943],
       [ 0.7565,  0.9449,  0.2796,  0.4703,  0.2926],
       [ 0.4143,  0.5891,  0.4370,  0.6060,  0.0161]])

b Parameter containing:
tensor([ 0.3592,  0.3455, -0.2517, -0.5678, -0.6016], :)
c Parameter containing:
tensor([-1.5490], requires_grad=True)
```

Before optimizer update

```
[61] # Gradient update:
    optimizer.step()
# After gradient update
    for name, param in model.named_parameters():
        print(name, param)
```

After optimizer update

```
A Parameter containing:
tensor([[-0.2167,  0.6621, -0.8093,  0.7623, -0.6556],
       [ 1.2510, -2.4280, -0.5512, -0.1244, -0.2787],
       [ 0.4892,  0.4643, -1.3430,  1.2834, -1.0043],
       [ 0.7465,  0.9349,  0.2696,  0.4803,  0.3026],
       [ 0.4043,  0.5791,  0.4270,  0.6160,  0.0261]])

b Parameter containing:
tensor([ 0.3492,  0.3355, -0.2617, -0.5578, -0.5916], :)
c Parameter containing:
tensor([-1.5390], requires_grad=True) 33
```

# Many Different Update Rules

- **Simple SGD:** update with only gradients
- **Momentum:** update w/ running average of gradient
- **Adagrad:** update downweighting high-variance values
- **Adam:** update w/ running average of gradient, downweighting by running average of variance

# Standard SGD

- **Reminder:** Standard stochastic gradient descent does

$$g_t = \frac{\nabla_{\theta_{t-1}} \ell(\theta_{t-1})}{\text{Gradient of Loss}}$$

$$\theta_t = \theta_{t-1} - \frac{\eta g_t}{\text{Learning Rate}}$$

- There are many other optimization options! (see Ruder 2016 in references)

# SGD With Momentum

- Remember gradients from past time steps

$$v_t = \gamma v_{t-1} + \eta g_t$$

—      —      —

Momentum      Momentum      Previous Momentum  
Conservation  
Parameter

$$\theta_t = \theta_{t-1} - v_t$$

- Intuition:** Prevent instability resulting from sudden changes

# Adagrad

- Adaptively reduce learning rate based on accumulated variance of the gradients

$$G_t = G_{t-1} + g_t \odot g_t$$

Squared Current Gradient

$$\theta_t = \theta_{t-1} - \frac{\eta}{\sqrt{G_t + \epsilon}} g_t$$

— Small Constant

- **Intuition:** frequently updated parameters (e.g. common word embeddings) should be updated less
- **Problem:** learning rate continuously decreases, and training can stall -- fixed by using rolling average in *AdaDelta* and *RMSProp*

# Adam

- Most standard optimization option in NLP and beyond
- Considers rolling average of gradient, and momentum

$$m_t = \beta_1 m_{t-1} + (1 - \beta_1) g_t \quad \text{Momentum}$$

$$v_t = \beta_2 v_{t-1} + (1 - \beta_2) g_t \odot g_t \quad \text{Rolling Average of Gradient}$$

- Correction of bias early in training, because  $\mathbb{E}[v_t]$  is a biased estimation of variance:  $\mathbb{E}[v_t] = \mathbb{E}[g_t^2] \cdot (1 - \beta_2^t)$

$$\hat{m}_t = \frac{m_t}{1 - (\beta_1)^t} \quad \hat{v}_t = \frac{v_t}{1 - (\beta_2)^t}$$

- Final update

$$\theta_t = \theta_{t-1} - \frac{\eta}{\sqrt{\hat{v}_t} + \epsilon} \hat{m}_t$$

# Training Tricks

# Shuffling the Training Data

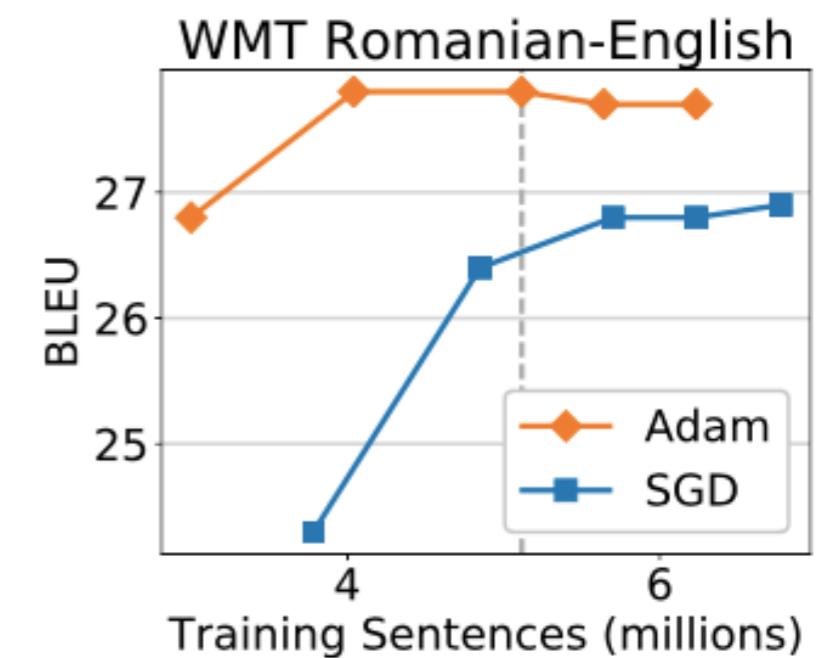
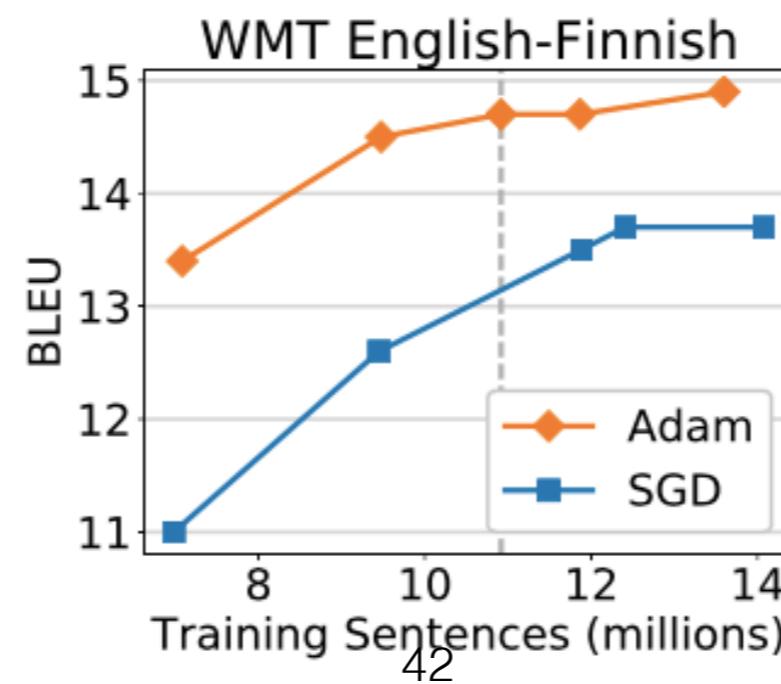
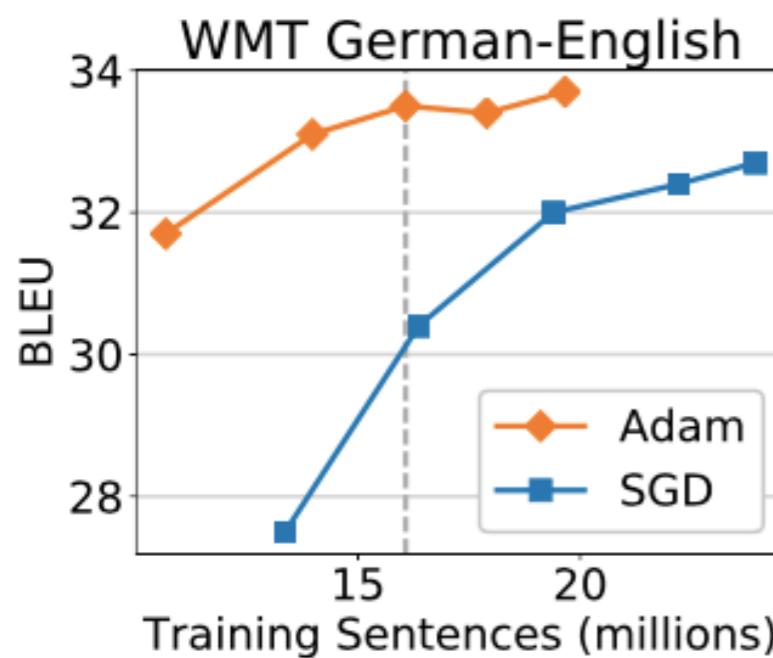
- Stochastic gradient methods update the parameters a little bit at a time
  - What if we have the sentence “I love this sentence so much!” at the end of the training data 50 times?
- To train correctly, we should randomly shuffle the order at each time step

# Simple Methods to Prevent Over-fitting

- Neural nets have tons of parameters: we want to prevent them from over-fitting
- **Early stopping:**
  - monitor performance on held-out development data and stop training when it starts to get worse
- **Learning rate decay:**
  - gradually reduce learning rate as training continues, or
  - reduce learning rate when dev performance plateaus
- **Patience:**
  - learning can be unstable, so sometimes avoid stopping or decay until the dev performance gets worse  $n$  times

# Which One to Use?

- Adam is usually fast to converge and stable
- But simple SGD tends to do very well in terms of generalization (Wilson et al. 2017)
- You should use learning rate decay, (e.g. on Machine translation results by Denkowski & Neubig 2017)



# Dropout

(Srivastava+ 14)

- Neural nets have lots of parameters, and are prone to overfitting
- Dropout: randomly zero-out nodes in the hidden layer with probability  $p$  at **training time only**



- Because the number of nodes at training/test is different, scaling is necessary:
  - **Standard dropout:** scale by  $1-p$  at test time
  - **Inverted dropout:** scale by  $1/(1-p)$  at training time
- An alternative: **DropConnect** (Wan+ 2013) instead zeros out weights in the NN

# Efficiency Tricks: Operation Batching

# Efficiency Tricks: Mini-batching

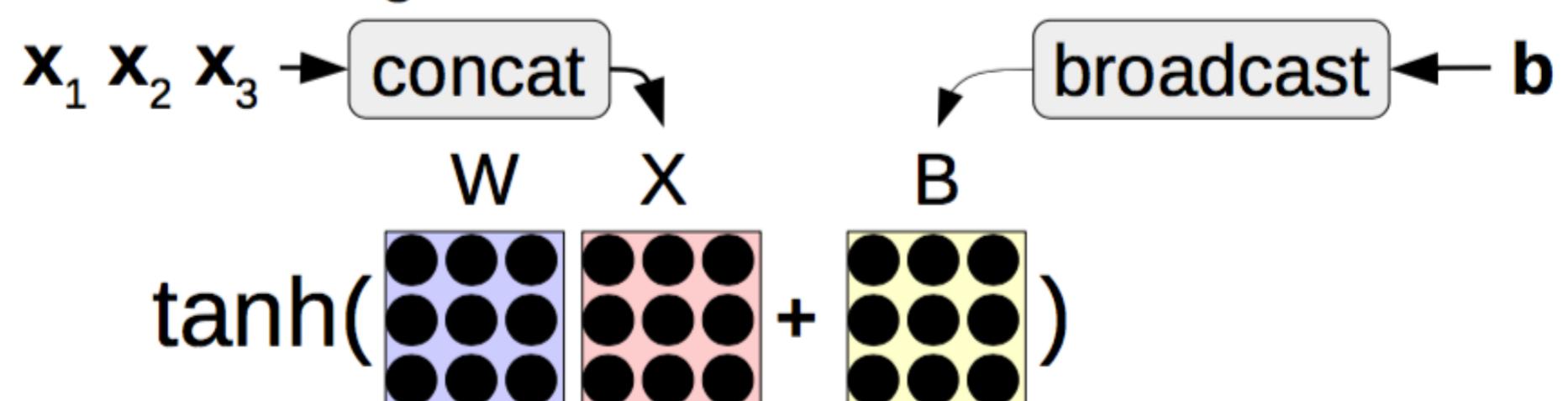
- On modern hardware 10 operations of size 1 is **much slower than** 1 operation of size 10
- Minibatching combines together smaller operations into one big one

# Minibatching

## Operations w/o Minibatching

$$\text{tanh}(\begin{matrix} \mathbf{W} & \mathbf{x}_1 & \mathbf{b} \\ \begin{matrix} \text{purple} \end{matrix} & \begin{matrix} \text{pink} \end{matrix} & \begin{matrix} \text{yellow} \end{matrix} \end{matrix} + \begin{matrix} \text{yellow} \end{matrix}) \quad \text{tanh}(\begin{matrix} \mathbf{W} & \mathbf{x}_2 & \mathbf{b} \\ \begin{matrix} \text{purple} \end{matrix} & \begin{matrix} \text{pink} \end{matrix} & \begin{matrix} \text{yellow} \end{matrix} \end{matrix} + \begin{matrix} \text{yellow} \end{matrix}) \quad \text{tanh}(\begin{matrix} \mathbf{W} & \mathbf{x}_3 & \mathbf{b} \\ \begin{matrix} \text{purple} \end{matrix} & \begin{matrix} \text{pink} \end{matrix} & \begin{matrix} \text{yellow} \end{matrix} \end{matrix} + \begin{matrix} \text{yellow} \end{matrix})$$

## Operations with Minibatching



# Procedure of Minibatching

- **Group together similar operations** (e.g. loss calculations for a single word) and execute them all together
  - In the case of a feed-forward language model, each word prediction in a sentence can be batched
  - For recurrent neural nets, etc., more complicated
- How this works depends on toolkit
  - Most toolkits have require you to **add an extra dimension** representing the batch size
  - Some toolkits have **explicit tools** that help with batching

# Assignment

# Still Some Things Left!

- We've left off the details of some underlying parts.
- What about more operations?
- What about more optimizers?
- **Challenge:** can you make a more sophisticated model?

<https://github.com/JunjieHu/cs769-assignments/tree/main/assignment1>

# Questions?