

CS639 Deep Learning for NLP

Long-context Language Modeling

Junjie Hu



Slides adapted from Zhengzhong, Graham
<https://junjiehu.github.io/cs639-spring26>

Goal for Today

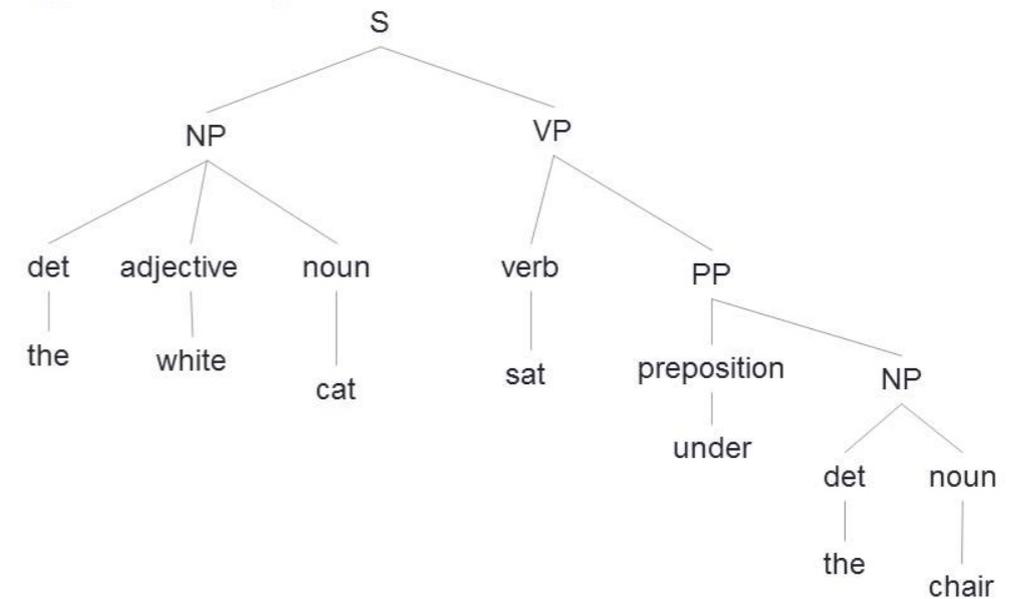
1. Long-Context Language Modeling
 - RNN-based Models
 - Transformer-based Models
2. Evaluating Long-context Understanding

Some NLP Tasks we've Handled

Alice was beginning to get very tired of sitting by her sister on the bank, and of having nothing to do: once or twice she had peeped into the book her sister was reading, but it had no pictures or conversations in it, 'and what is the use of a book,' thought Alice 'without pictures or conversation?'

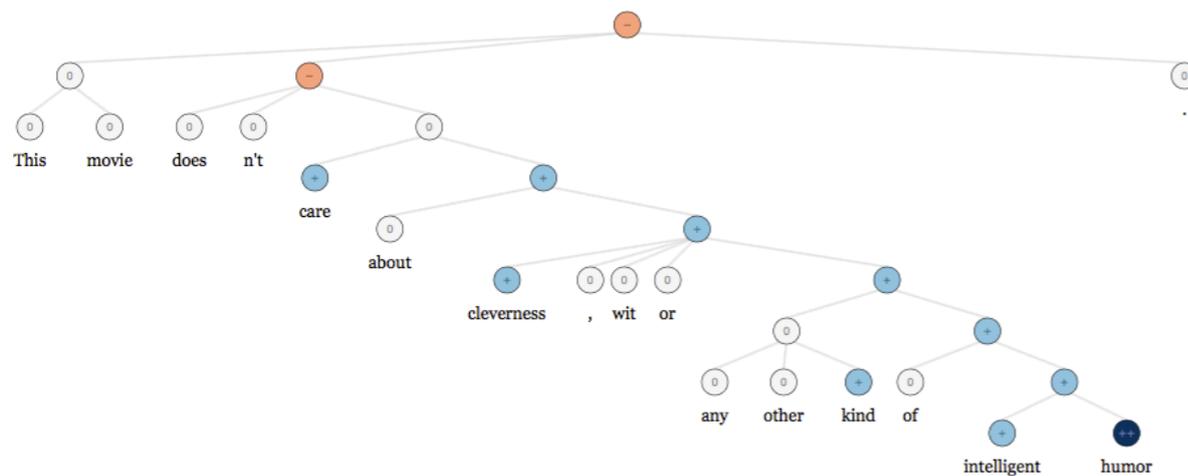
$P(w_{i+1} = \text{of} \mid w_i = \text{tired}) = 1$
 $P(w_{i+1} = \text{of} \mid w_i = \text{use}) = 1$
 $P(w_{i+1} = \text{sister} \mid w_i = \text{her}) = 1$
 $P(w_{i+1} = \text{beginning} \mid w_i = \text{was}) = 1/2$

$P(w_{i+1} = \text{bank} \mid w_i = \text{the}) = 1/3$
 $P(w_{i+1} = \text{book} \mid w_i = \text{the}) = 1/3$
 $P(w_{i+1} = \text{use} \mid w_i = \text{the}) = 1/3$



Language Models

Parsing



Classification

Germany's representative to the European Union's veterinary committee Werner Zwingman said on Wednesday consumers should ...

Entity Tagging

Why Long Context Matters?

- Many real-world tasks require reasoning over long text:
 - Legal documents
 - Scientific literature
 - Books and reports
 - Software repositories
 - Multi-document reasoning
- LLMs must integrate information across **thousands to millions of tokens**.

Some Connections to Tasks over Documents

Prediction using documents

- **Document-level language modeling:** Predicting language on the multi-sentence level (c.f. single-sentence language modeling)
- **Document classification:** Predicting traits of entire documents (c.f. sentence classification)

- **Entity coreference:** Which entities correspond to each-other? (c.f. NER)
- **Discourse parsing:** How do segments of a document correspond to each-other? (c.f. syntactic parsing)

Prediction of document structure

Context Window in LLMs

- The **context window** defines how many tokens the model can see.
- Increasing context length introduces **major computational challenges**.

Model Era	Context
Early Transformers	512 tokens
GPT-3	2k–4k
Recent LLMs	32k–128k
Newest models	1M+ tokens

Challenges of Long Context

- Major problems:
 - Quadratic attention cost especially for Transformer LLMs
 - GPU memory limits
 - Training long sequences
 - Modeling long-range dependencies
 - Evaluation difficulties
- These challenges drive active research.

Alice was beginning to get very tired of sitting by her sister on the bank, and of having nothing to do: once or twice she had peeped into the book her sister was reading, but it had no pictures or conversations in it, 'and what is the use of a book,' thought Alice 'without pictures or conversation?'

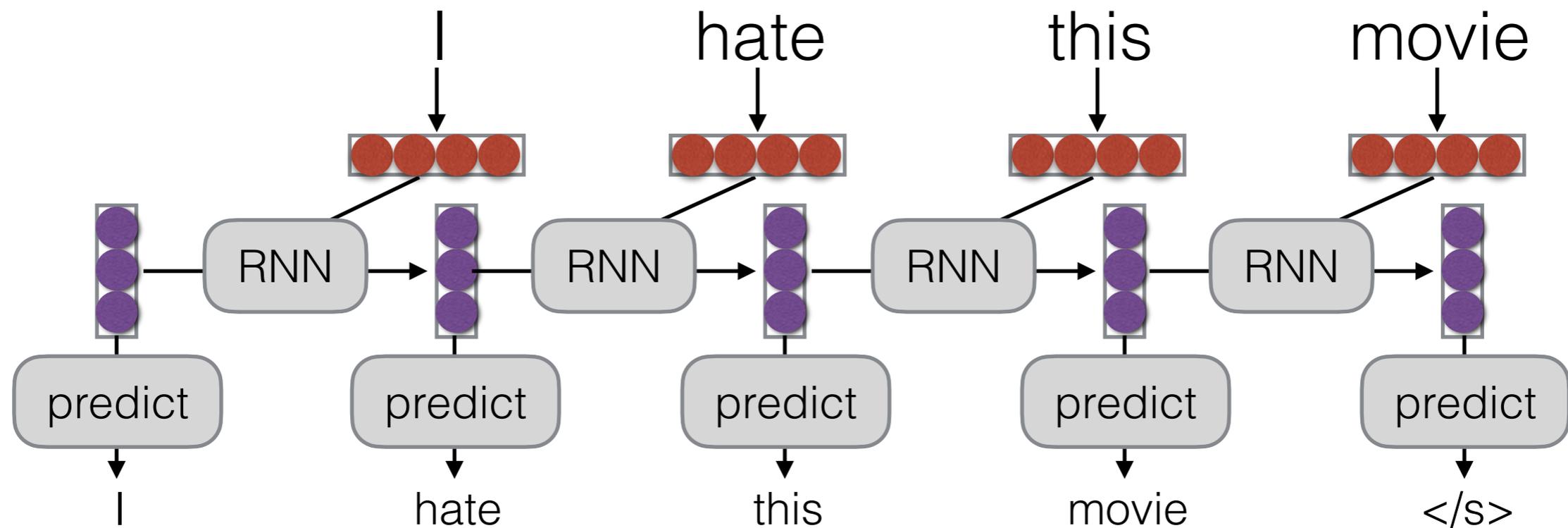
Long-Context Language Modeling

Long-Context Language Modeling

- We want to predict the probability of words in a long document
- Obviously sentences in a document don't exist in a vacuum! We want to take advantage of this fact.

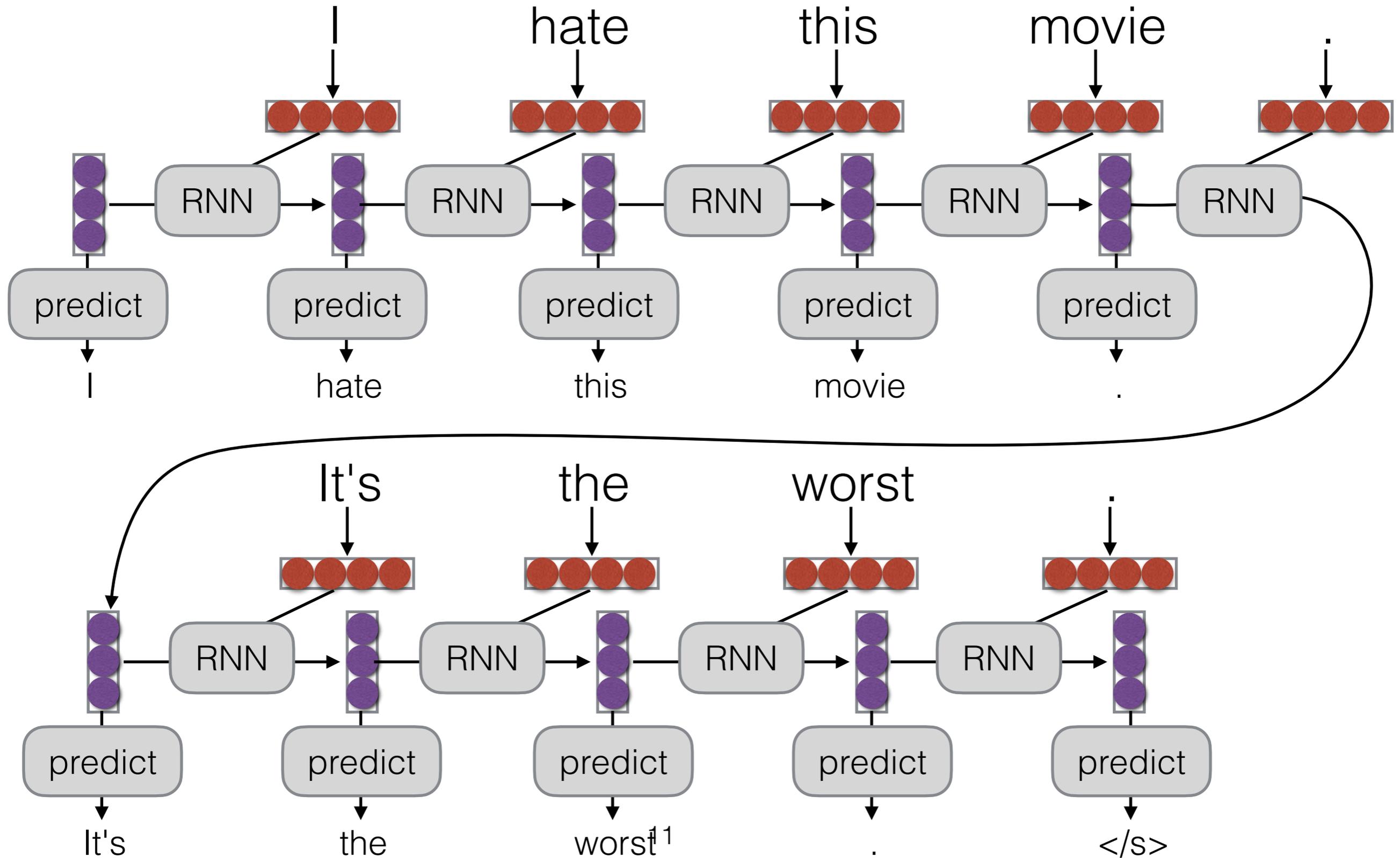
Remember: Modeling using Recurrent Networks

- Model passing previous information in hidden state



Simple: Infinitely Pass State by RNN LM

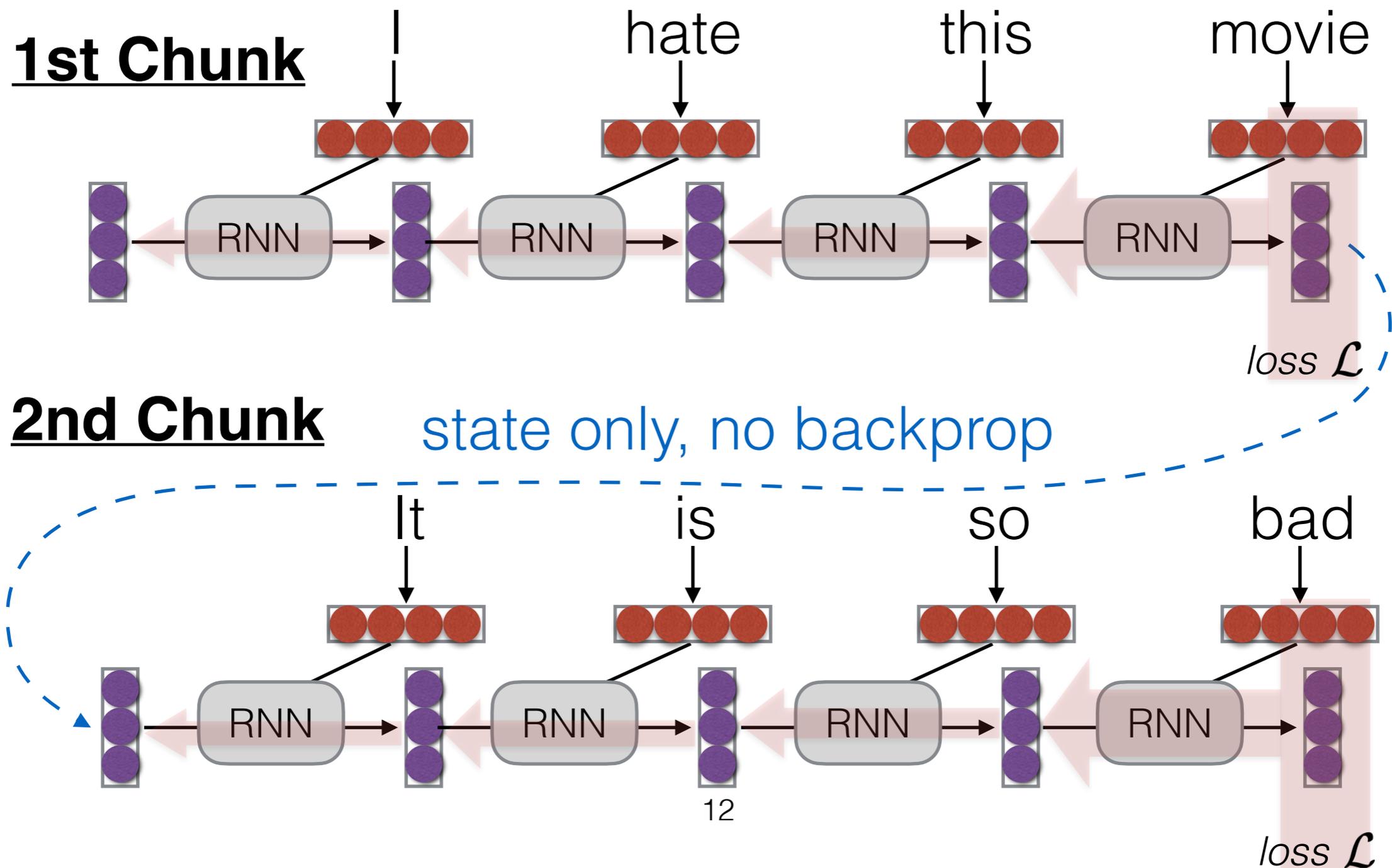
(Mikolov et al. 2011)



Truncated Backpropagation Through Time (TBPTT)

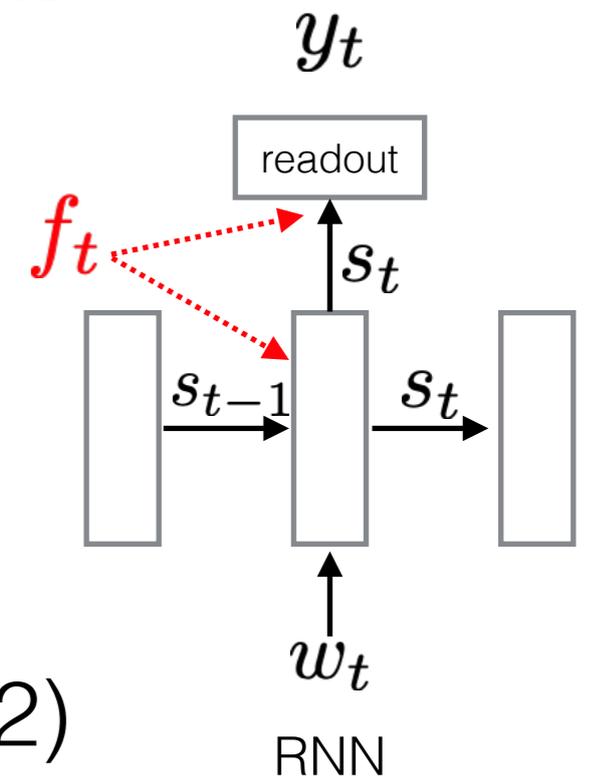
(Elman 1990, Boden 2001)

- The backpropagation update is performed back for a fixed number of past time steps.



Separate Encoding for Coarse-grained Document Context

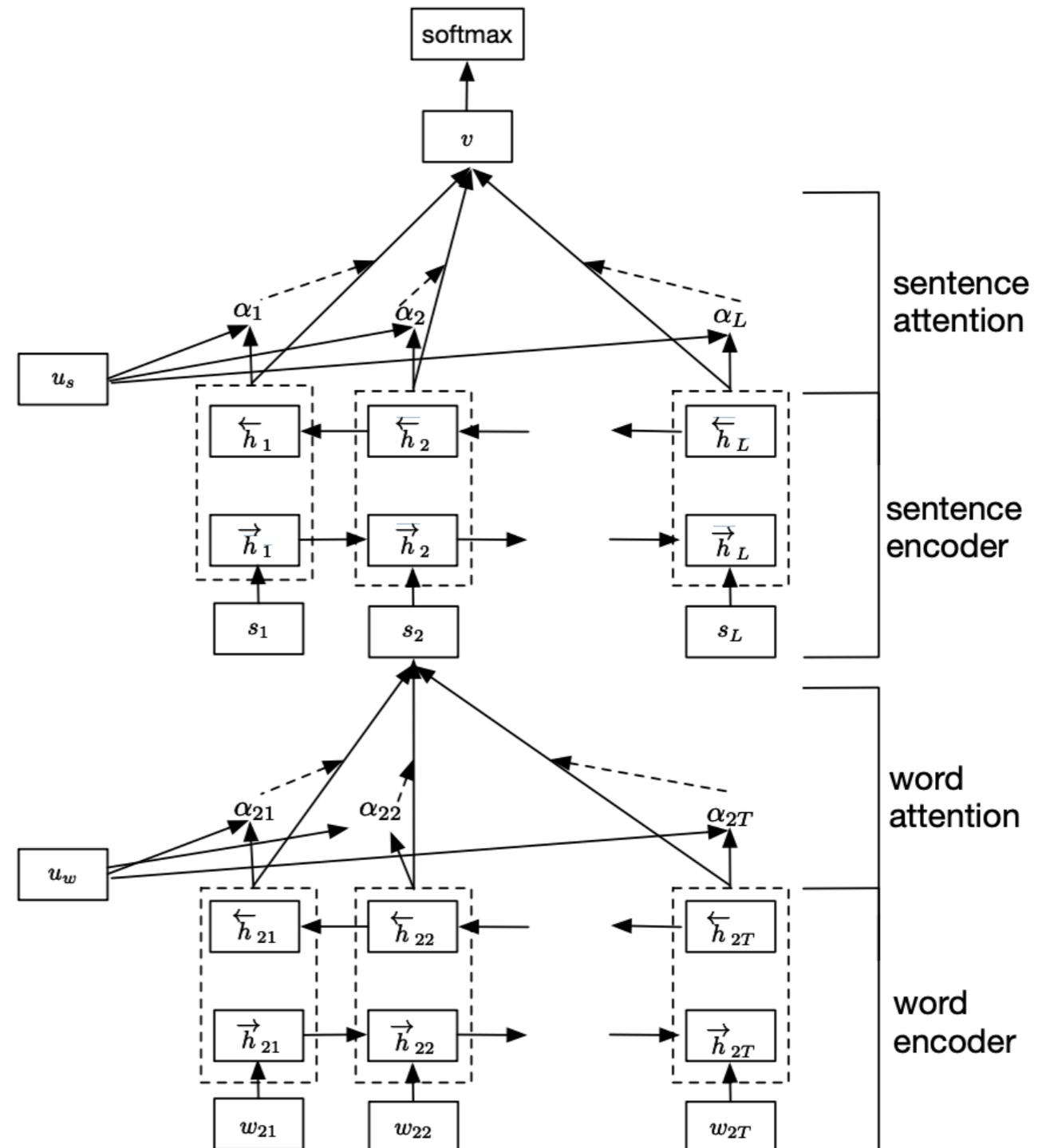
- Explicitly add the external global features f_t as input to
 1. each RNN cell
 2. The final readout linear layer
- What global context?
 - Use topic modeling (Mikolov & Zweig 2012)
 - Use bag-of-words of previous sentence(s), optionally with attention (Wang and Cho 2016)
 - Use last state of previous sentence (Ji et al. 2015)



Hierarchical Attention Network

(Yang et al. 2018)

- One word-level BiGRU to encode words within a sentence
- Learn a weighted sum of word hidden vectors as the sentence representation.
- One sentence-level BiGRU to encode sentences within a document
- Weighted sum of sentence hidden vectors as the doc representation.



Transformer-based Methods (Attention Matrix)

Transformer Self-Attention

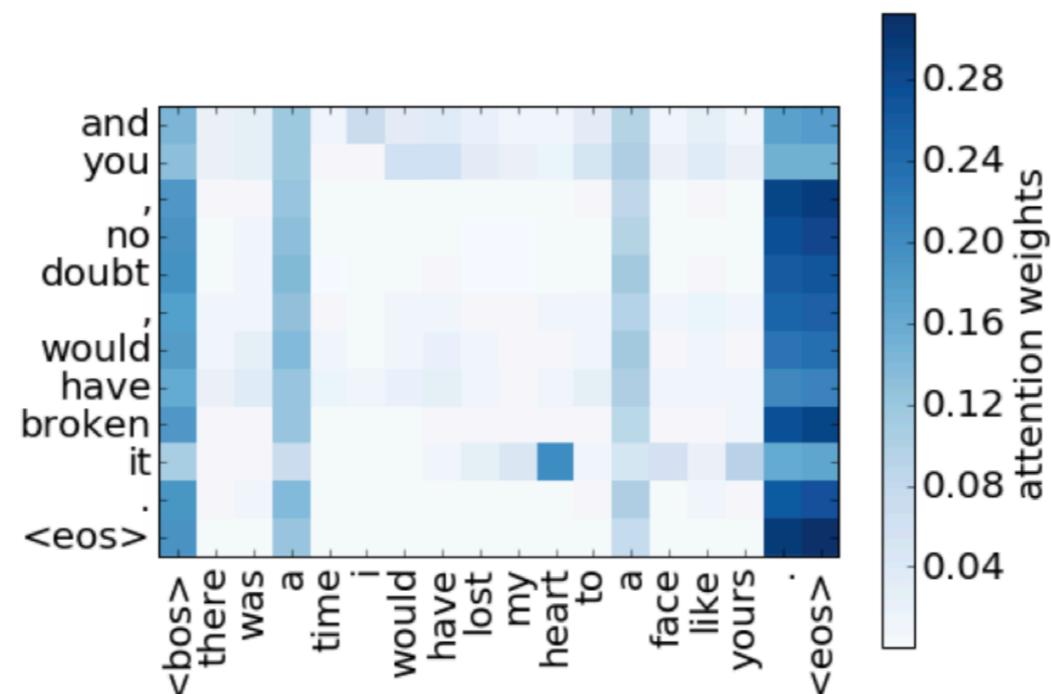
- Transformers rely on **self-attention**:
 - Each token attends to all other tokens.
 - Attention weight:

$$\text{softmax}(QK^T / \sqrt{d})$$

- This enables flexible contextual reasoning, but both $Q, K \in \mathbb{R}^{d \times L}$

Transformers Across Sentences

- Simply self-attend to all words in the document
 - + Can simply use document-level context
 - + Can learn interesting phenomena (e.g. co-reference)



- - Computation of the attention matrix is quadratic in sequence length $O(L^2)$!

Attention Complexity

- Self-attention leads to **quadratic complexity** both in **compute** and **memory**

Example:

Tokens	Attention Matrix
1k	1M entries
100k	10B entries

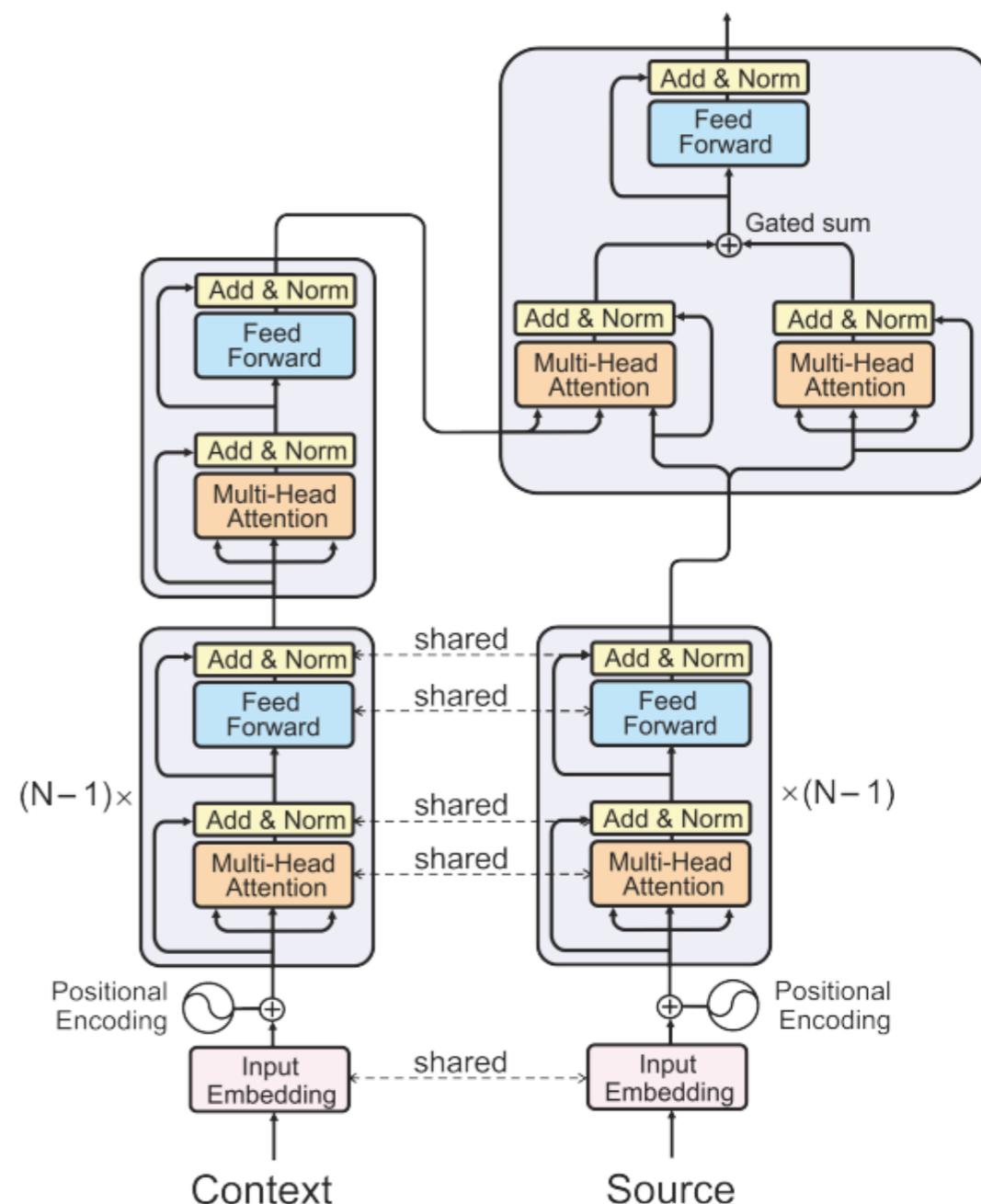
- This becomes infeasible for long sequences.

Long Context Research Directions

- Main approaches:
 - Efficient attention mechanisms
 - Sparse attention
 - Linear attention
 - Retrieval-based methods
 - External memory
 - Training techniques

Encode Context and Source Separately (Elena et al. 2018)

- Use two Transformer encoders to encode the **context and current source sentence separately** instead of a combined document.
- Share the first $N-1$ layers for the two encoders.
- Context: previous/next sentence, or random sentence in the doc
- + Reduce the computation from quadratic of **doc length** $O(L^2)$ to quadratic of **sentence length** $O(l^2)$

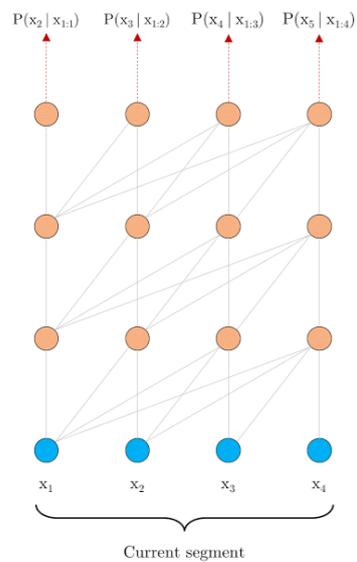


Transformer-XL: Truncated BPTT+Transformer

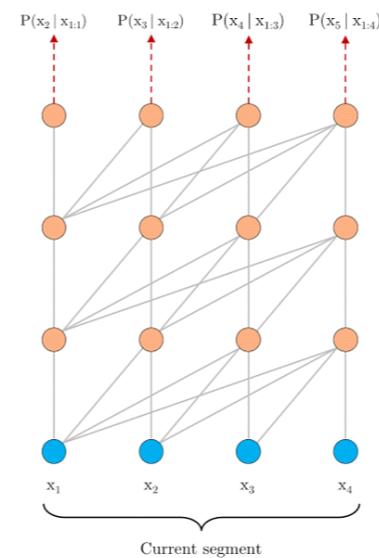
(Dai et al. 2019)

- Standard Transformer: encode each chunk separately
- Transformer-XL: attend to fixed **vectors** from the previous sentence

Standard Transformer



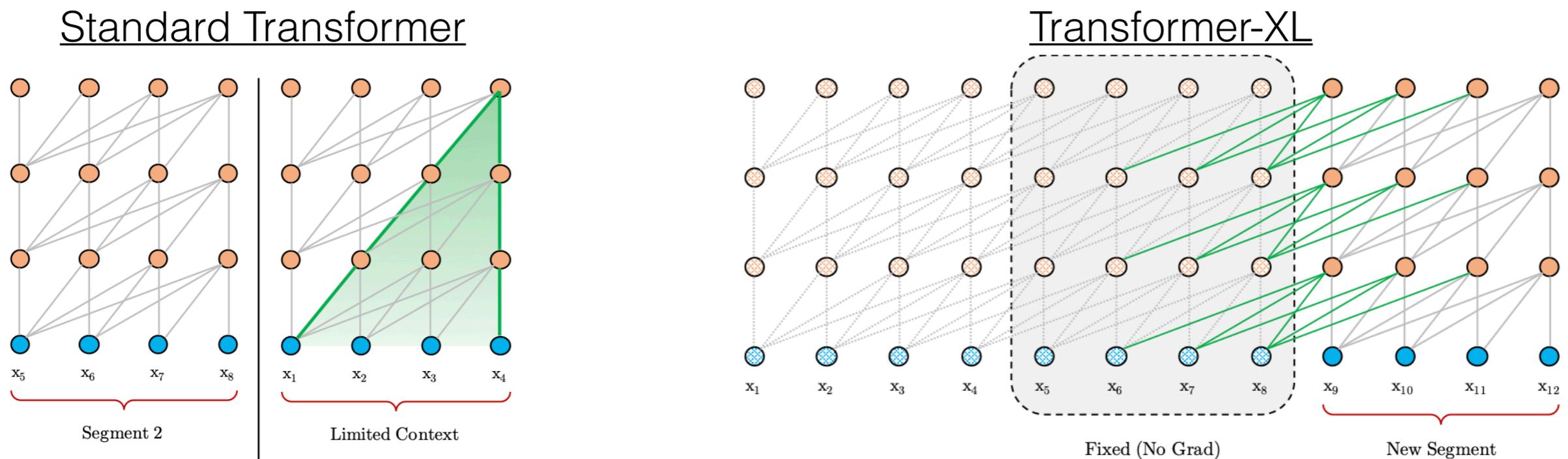
Transformer-XL



Transformer-XL: Truncated BPTT+Transformer

(Dai et al. 2019)

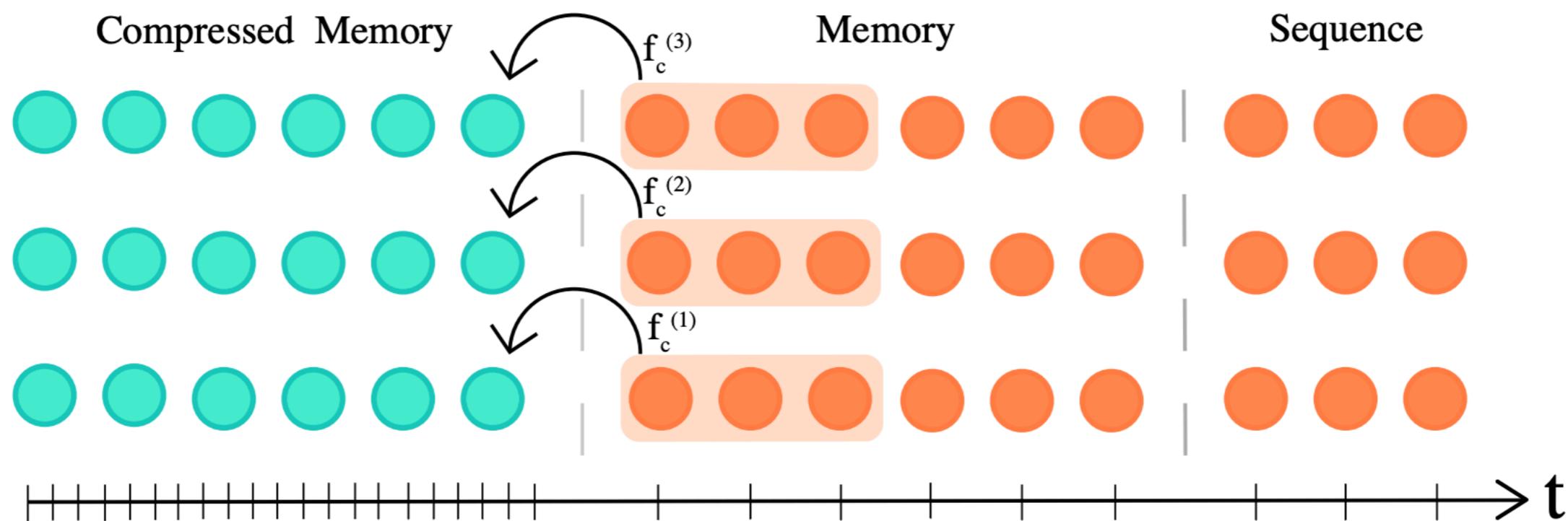
- Like truncated backprop through time for RNNs; can use previous states, but not backprop into them



- How far away can Transformer-XL look back?
 - $O(N \times l)$, N is the no. of layers, l is the no. of words in a chunk

Compressing Previous States

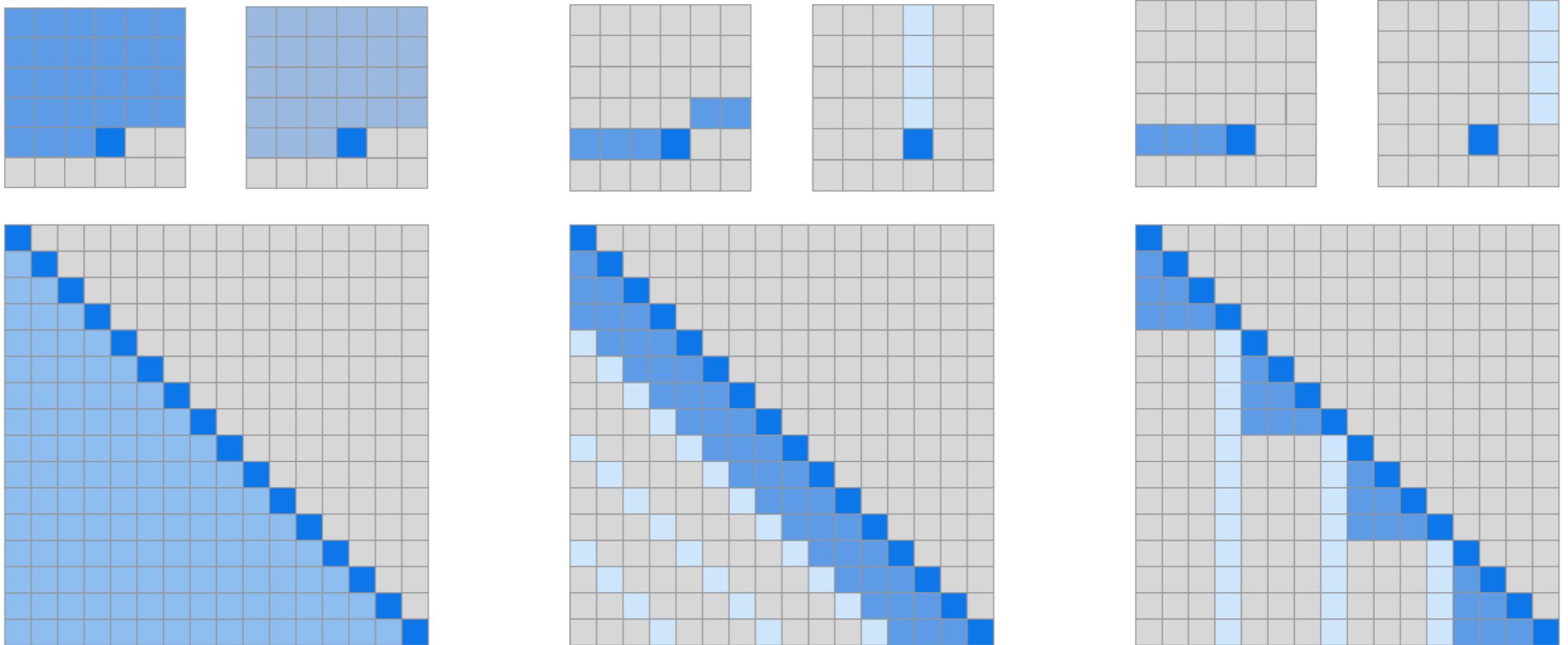
- Extension over Transformer-XL that uses the last chunk as the memory
- Add a "strided" compression step over previous states (Rae & Potapenko et al. 2019)



Sparse Transformers

(Child et al. 2019)

- Add "stride", only attending to every n previous states



(a) Transformer

(b) Sparse Transformer (strided)

(c) Sparse Transformer (fixed)

Adaptive Span Transformers

- Can make the span adaptive attention head by attention head some are short, some long (Sukhbaatar et al. 2019)

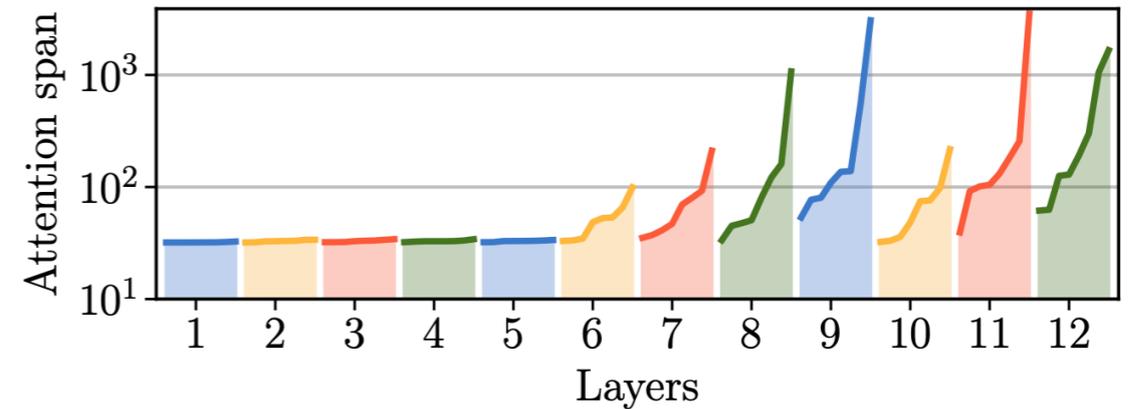
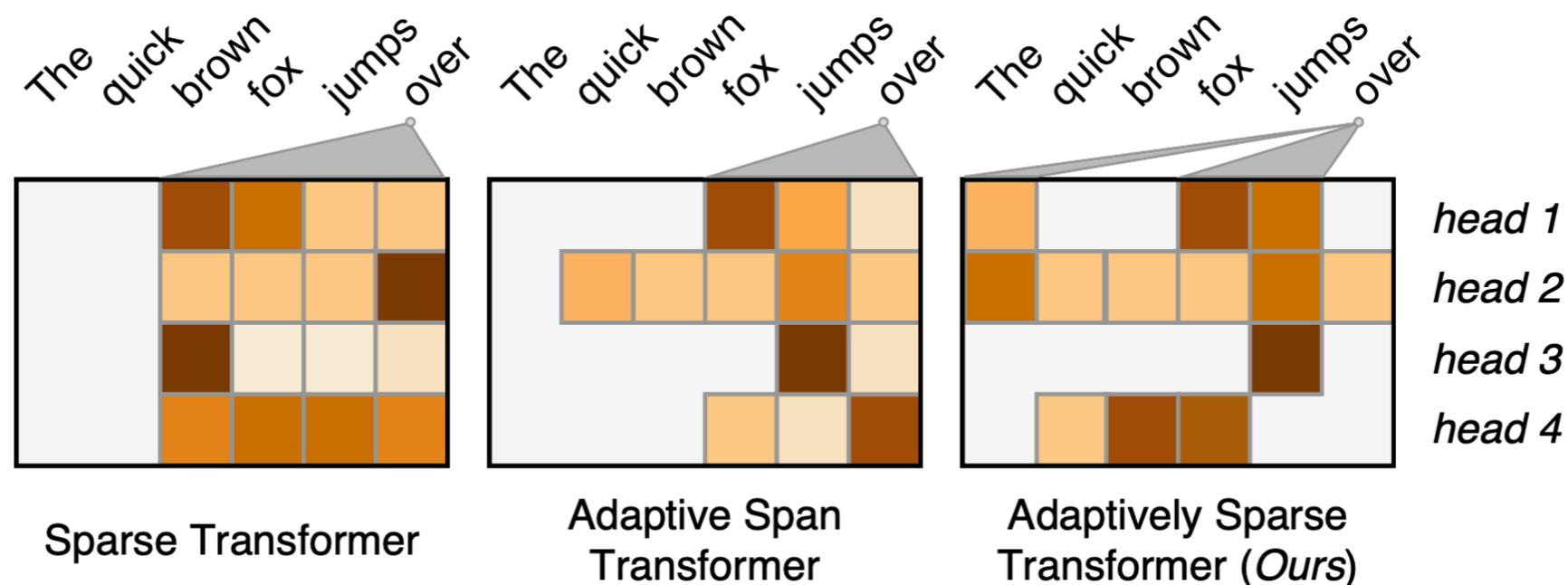


Figure 4: Adaptive spans (in log-scale) of every attention heads in a 12-layer model with span limit $S = 4096$. Few attention heads require long attention spans.

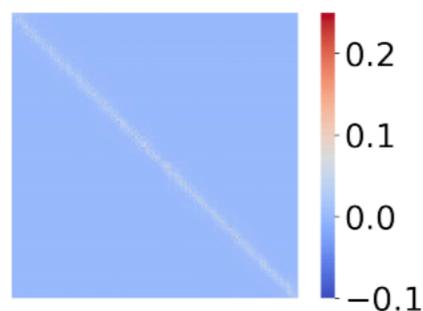
- Can be further combined with sparse computation (Correira et al. 2019)



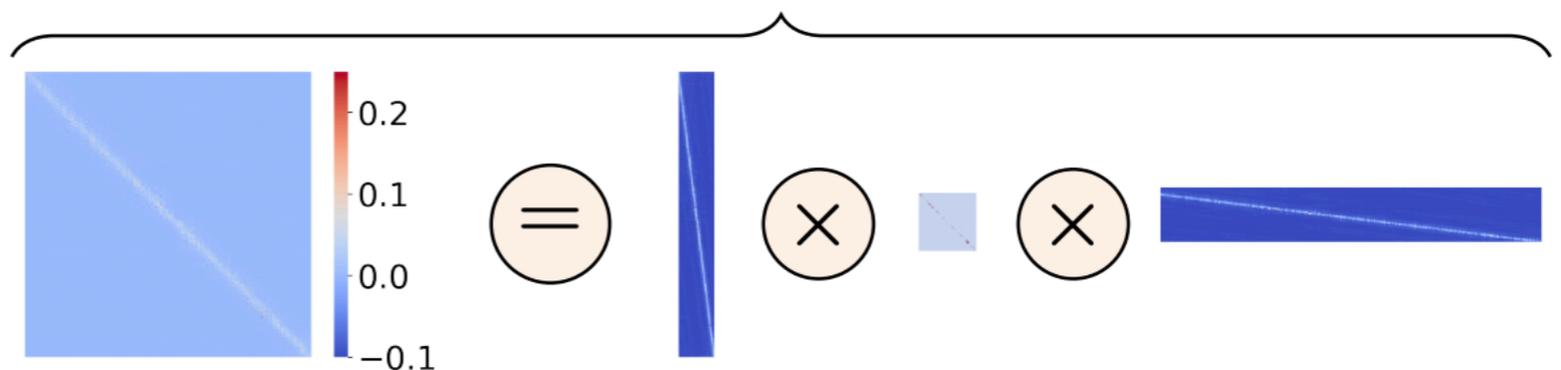
Low-rank Approximation

- Calculating the attention matrix is expensive, can it be predicted with a low-rank matrix?
- **Linformer:** Add low-rank linear projections into model (Wang et al. 2020)
- **Nystromformer:** Approximate using the Nystrom method, sampling "landmark" points (Xiong et al. 2021)

softmax



Nyström approximation



Summary of Training-time Methods

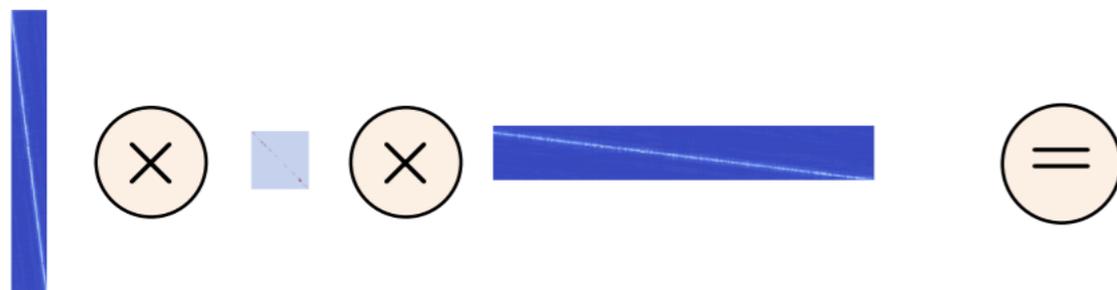
- The current bottleneck of Transformer-based model for long sequences is the **computation of attention matrix**

- Attend to past memory

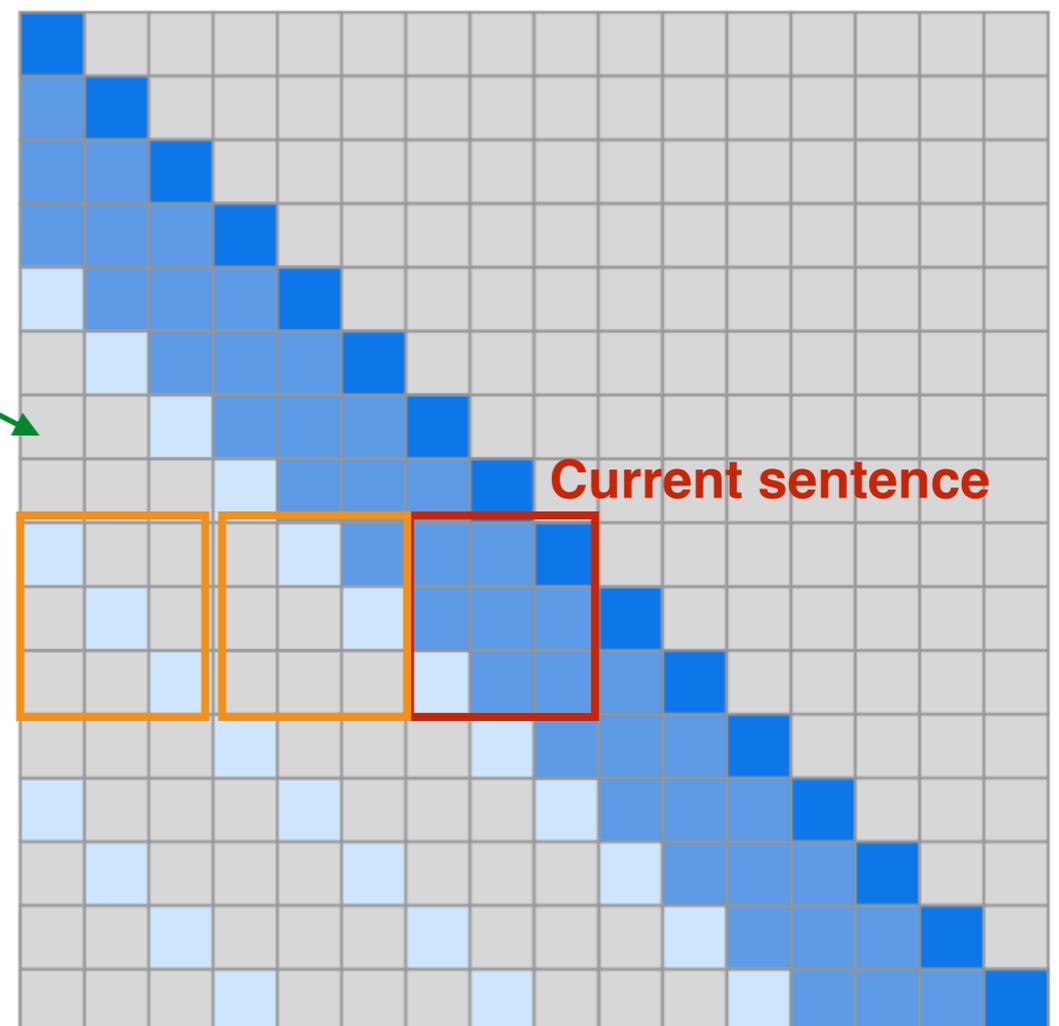
- Sparse assumption

- Low-rank approximation

- ...



Memory

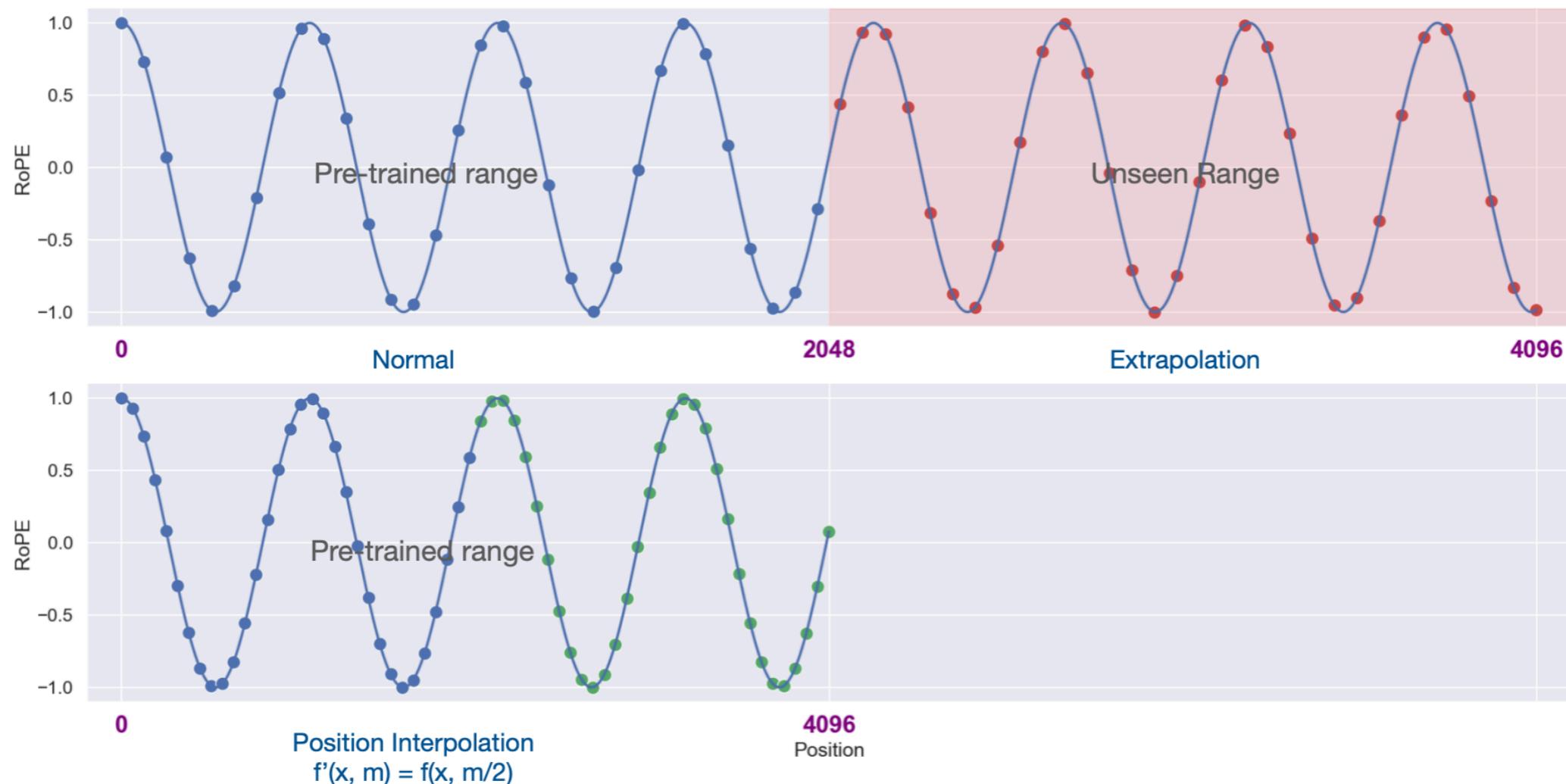


Long-Context Language Modeling **at Inference**

- During pre-training, large language models (LLMs) are often using **full attention and a length limit** (i.e., without any modification to their attentions).
- What about extending the context length limit of a **trained LLM at inference**?
 - **Position Interpolation**: estimate the position embedding out of the maximum length limit
 - **KV Cache**: cache the important key-value pairs from the attention in the memory

Length Extension at Inference

- Position Interpolation: What about extending the context length of a **trained LLM at inference**?

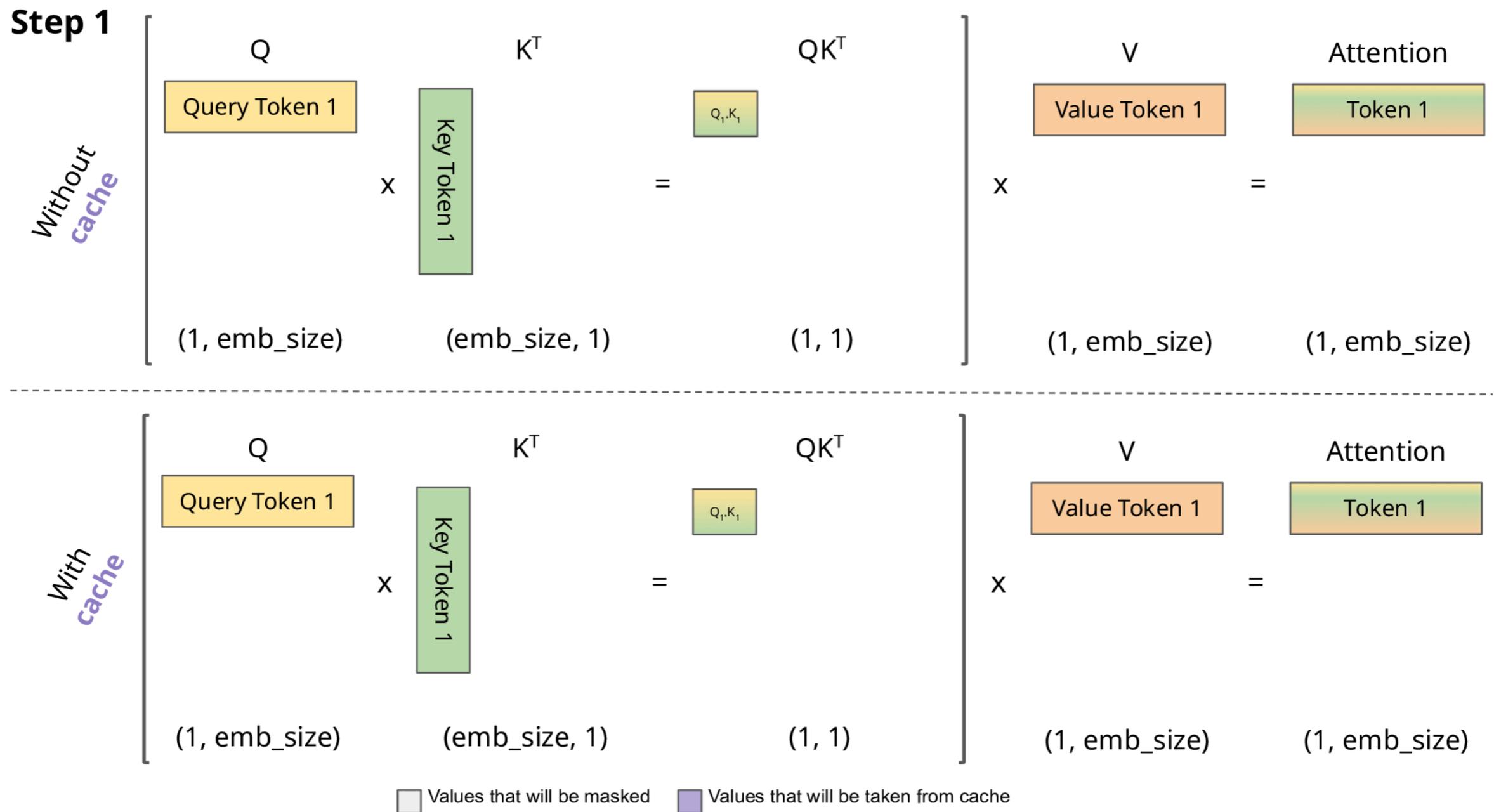


$$\mathbf{f}'(\mathbf{x}, m) = \mathbf{f}\left(\mathbf{x}, \frac{mL}{L'}\right).$$

$f()$ is the function that takes in a word embedding x , and a position index, and returns an embedding with positional information

KV Cache

- Cache the computed key-value pairs from the long context



Evaluation and Long-Context Tasks

How to Evaluate Document-level Models?

- Simple: Perplexity, classification over long documents
- More focused:
 - Sentence scrambling (Barzilay and Lapata 2008)
 - Final sentence prediction (Mostafazadeh et al. 2016)
 - Final word prediction (Paperno et al. 2016)
- Composite benchmark containing several task: Long range arena (Tay et al. 2020)

Needle-in-a-Haystack

- Multi-document QA task: retrieve the correct answer from an long text string and measure the accuracy

Input Context

Write a high-quality answer for the given question using only the provided search results (some of which might be irrelevant).

Document [1] (Title: Asian Americans in science and technology) Prize in physics for discovery of the subatomic particle J/ψ . Subrahmanyan Chandrasekhar shared...

Document [2] (Title: List of Nobel laureates in Physics) The first Nobel Prize in Physics was awarded in 1901 to Wilhelm Conrad Röntgen, of Germany, who received...

Document [3] (Title: Scientist) and pursued through a unique method, was essentially in place. Ramón y Cajal won the Nobel Prize in 1906 for his remarkable...

Question: who got the first nobel prize in physics

Answer:

Desired Answer

Wilhelm Conrad Röntgen

Needle-in-a-Haystack

- Retrieving string in a JSON object.

Input Context

Extract the value corresponding to the specified key in the JSON object below.

JSON data:

```
{ "2a8d601d-1d69-4e64-9f90-8ad825a74195": "bb3ba2a5-7de8-434b-a86e-a88bb9fa7289",  
  "a54e2eed-e625-4570-9f74-3624e77d6684": "d1ff29be-4e2a-4208-a182-0cea716be3d4",  
  "9f4a92b9-5f69-4725-ba1e-403f08dea695": "703a7ce5-f17f-4e6d-b895-5836ba5ec71c",  
  "52a9c80c-da51-4fc9-bf70-4a4901bc2ac3": "b2f8ea3d-4b1b-49e0-a141-b9823991ebeb",  
  "f4eb1c53-af0a-4dc4-a3a5-c2d50851a178": "d733b0d2-6af3-44e1-8592-e5637fdb76fb" }
```

Key: "**9f4a92b9-5f69-4725-ba1e-403f08dea695**"

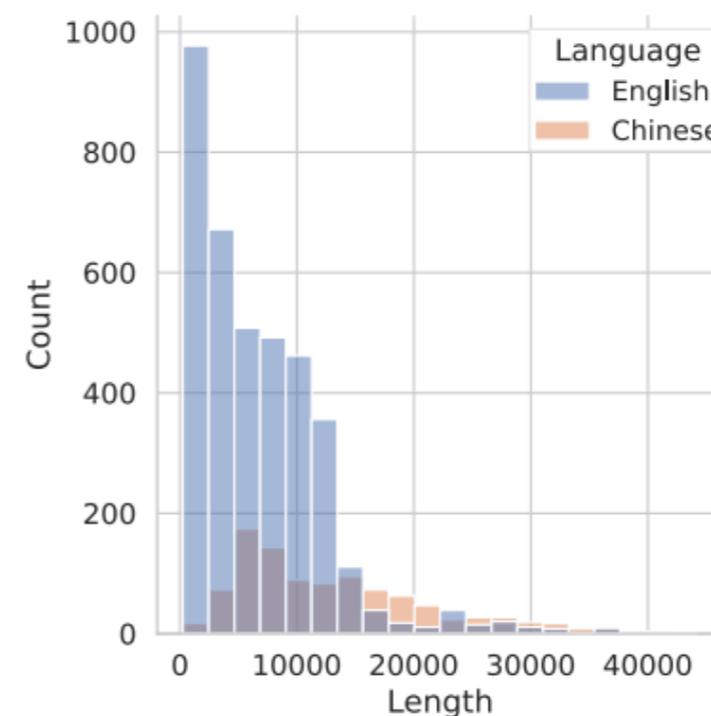
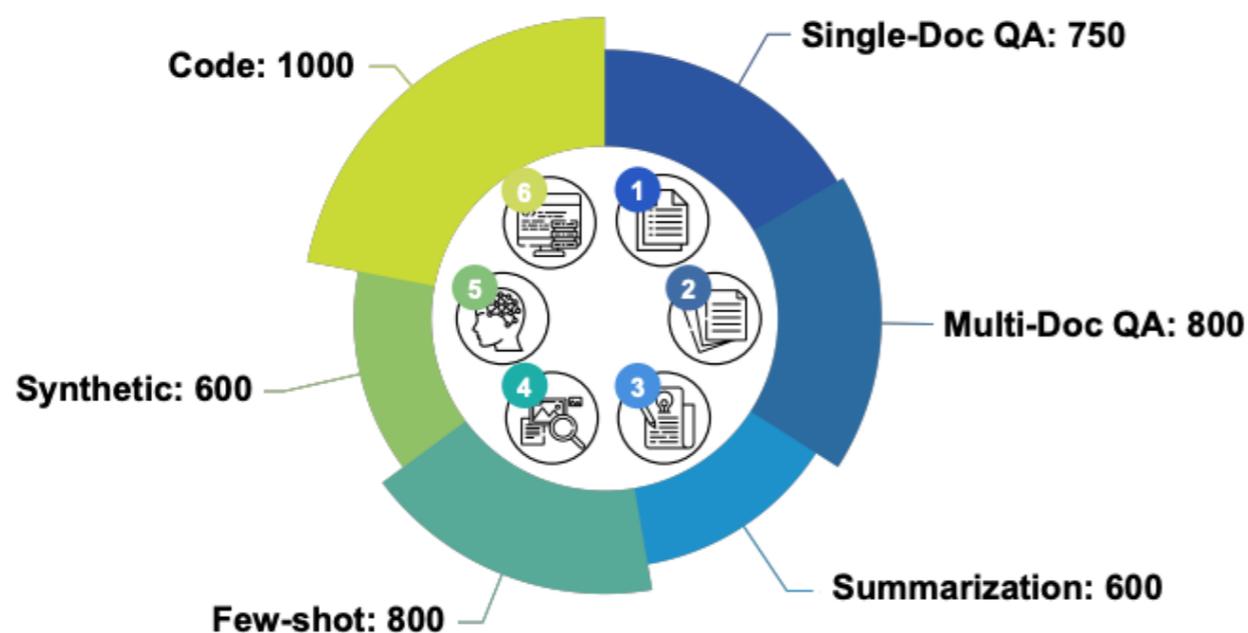
Corresponding value:

Desired Output

```
703a7ce5-f17f-4e6d-b895-5836ba5ec71c
```

LongBench

- A bilingual, multi-task benchmark for evaluating LLMs in handling extended documents and complex information sequences.



LongBench

NarrativeQA: You are given a story, which can be either a novel or a movie script, and a question. Answer the question as concisely as you can, using a single phrase if possible. Do not provide any explanation.

Story: {context}

Now, answer the question based on the story as concisely as you can, using a single phrase if possible.

Do not provide any explanation.

Question: {input}

Answer:

QMSum: You are given a meeting transcript and a query containing a question or instruction. Answer the query in one or more sentences.

Transcript:

{context}

Now, answer the query based on the above meeting transcript in one or more sentences.

Query: {input}

Answer:

Questions?